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NARODOWA STRATEGIA SPÓJNOŚCI

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„Image Processing and Computer Graphics”

Prezentacja multimedialna współfinansowana przez Unię Europejską w ramach Europejskiego Funduszu Społecznego w projekcie pt. „Innowacyjna dydaktyka bez ograniczeń - zintegrowany rozwój Politechniki Łódzkiej - zarządzanie Uczelnią, nowoczesna oferta edukacyjna i wzmacniania zdolności do zatrudniania osób niepełnosprawnych”

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Contribution Image Processing & Computer Graphics 2

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3D vector graphics Image Processing & Computer Graphics 3

- Co-ordinate systems
- Projection and transformation (linear algebra)
- Light and shading
- Rendering methods

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The image shows a screenshot of the Wikipedia article for '3D modeling'. The page title is '3D modeling' and it is identified as a Wikipedia article. The main content area includes a notice that the article does not cite any references or sources, followed by a paragraph explaining that 3D modeling is the process of developing a mathematical, wireframe representation of any three-dimensional object (either animate or inanimate) via specialized software. A sidebar on the right lists 'Basics' such as 3D modeling / 3D scanning, 3D rendering / 3D printing, and 3D computer graphics software, along with 'Primary Uses' like 3D models / Computer-aided design, Graphic design / Video games, Visual effects / Visualization, and Virtual engineering / Virtual reality. A navigation sidebar on the left contains links for 'Main page', 'Contents', 'Featured content', 'Current events', 'Random article', and 'Arch', along with a search bar and a 'Go' button.

This slide, titled '3D vector graphics', is part of a presentation on 'Image Processing & Computer Graphics'. It features a bulleted list of topics: 3D Objects, Surface description, Surface faces (usually triangles), Light and shading, 3D space, 3D space transformation, and 3D space projection. A central diagram illustrates a 3D model of a car on a grid, with projection lines extending from the car to a computer monitor and a tablet, demonstrating the projection process. The slide footer includes logos for 'KAPITAL LUDZKI' and the 'Unia Europejska' (European Union) with the text 'Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego'.

This slide, titled 'Co-ordinate systems', is part of a presentation on 'Image Processing & Computer Graphics'. It lists four coordinate systems: Object co-ordinate system, World co-ordinate system (WCS), Camera co-ordinate system (CCS), and Film co-ordinate system (FCS). It also includes 'Affine transformation' and 'Projection'. A diagram shows a 3D model of a car with three coordinate systems: WCS (World Co-ordinate System), CCS (Camera Co-ordinate System), and FCS (Film Co-ordinate System). The WCS axes are labeled X_{WCS} , Y_{WCS} , and Z_{WCS} . The CCS axes are labeled X_{CCS} , Y_{CCS} , and Z_{CCS} . The FCS axes are labeled X_{FCS} , Y_{FCS} , and Z_{FCS} . The slide footer includes logos for 'KAPITAL LUDZKI' and the 'Unia Europejska' (European Union) with the text 'Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego'.

Wikipedia article: **Projection (linear algebra)**

From Wikipedia, the free encyclopedia

"Orthogonal projection" redirects here. For the technical drawing concept, see *orthographic projection*. For a concrete discussion of orthogonal projections in finite-dimensional linear spaces, see *vector projection*.

In linear algebra and functional analysis, a **projection** is a linear transformation P from a vector space to itself such that $P^2 = P$. It leaves its image unchanged.^[1] Though abstract, the definition of "projection" formalizes and generalizes the idea of *graphical projection*. One can also consider the effect of a projection on a geometrical object by examining the effect of the projection on points in the object.

The transformation P is the orthogonal projection onto the line m .

Contents (hide)

- 1 Simple example
 - 1.1 Orthogonal projection
 - 1.2 Oblique projection
- 2 Classification
 - 2.1 Orthogonal projections
 - 2.2 Oblique projections
- 3 Projections on normed vector spaces
- 4 Applications and further considerations
- 5 See also
- 6 Notes
- 7 References
- 8 External links

Simple example [edit]

Orthogonal projection [edit]

For example, the function which maps the point (x, y, z) in three-dimensional space \mathbb{R}^3 to the point $(x, y, 0)$ is a projection onto the xy -plane.



Wikipedia article: **Graphical projection**

From Wikipedia, the free encyclopedia

For other uses, see *projection*.

Graphical projection is a protocol by which an image of an imaginary three-dimensional object is projected onto a planar surface without the aid of mathematical calculation.

Contents (hide)

- 1 Overview
- 2 Types of projection
 - 2.1 Orthographic projection
 - 2.1.1 Isometric
 - 2.1.2 Dimetric
 - 2.1.3 Trimetric
 - 2.2 Oblique projection
 - 2.3 Perspective
- 3 See also
- 4 References

Overview [edit]

The projection is achieved by the use of imaginary "projectors". The projected, mental image becomes the technician's vision of the desired, finished picture. By following the protocol the technician may produce the envisioned picture on a planar surface such as drawing paper. The protocols provide a uniform imaging procedure among people trained in technical graphics (mechanical drawing, computer aided design, etc.).

There are three types of graphical projection, categories each with its own protocol:

- orthographic projection
- oblique projection and
- perspective projection.



Wikipedia article: **Graphical projection**

Overview [edit]

The projection is achieved by the use of imaginary "projectors". The projected, mental image becomes the technician's vision of the desired, finished picture. By following the protocol the technician may produce the envisioned picture on a planar surface such as drawing paper. The protocols provide a uniform imaging procedure among people trained in technical graphics (mechanical drawing, computer aided design, etc.).

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- oblique projection and
- perspective projection.

Types of projection [edit]

Orthographic projection [edit]

The *Orthographic projection* is derived from the principles of *descriptive geometry* and may produce an image of an object as viewed from any direction of space. It is a parallel projection (the lines of projection are parallel both in reality and in the projection plane). It is the projection type of choice for working drawings.

Within orthographic projection there is an ancillary category known as "pictorials". Pictorials show an image of an object as viewed from a slant direction in order to reveal all three directions (axes) of space in one picture. Because pictorial projections inevitably contain this distortion, in the role, drawing instrument for pictorials, some liberties may be taken for economy of effort and best effect. Orthographic pictorials rely upon the technique of *axonometric projection*.



Image Processing & Computer Graphics 10

Projection Classification

```

    graph TD
      A[Planar Geometric Projections] --> B[Parallel]
      A --> C[Perspective]
      B --> D[Orthographic]
      B --> E[Other]
      D --> F["Top (Plan)"]
      D --> G[Front]
      D --> H[Side elevation]
      D --> I[Axonometric]
      I --> J[Isometric]
      I --> K[Other]
      C --> L[One-point]
      C --> M[Two-point]
      C --> N[Three-point]
  
```

„Introduction to Computer Graphics“
J.Foley, A. Van Dam, S. Feiner, R. Phillips
Addison-Wesley Pub. Comp. 1995

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Projection

- Co-ordinates of objects are given in CCS (already transformed).
- Projection is to reduce dimensionality of 3D space to 2D space (of a film)

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Wikipedia article: Orthogonal projection

Orthogonal projection

For example, the function which maps the point (x, y, z) in three-dimensional space \mathbb{R}^3 to the point $(x, y, 0)$ is a projection onto the xy -plane. This function is represented by the matrix:

$$P = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}.$$

The action of this matrix on an arbitrary vector is

$$P \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x \\ y \\ 0 \end{pmatrix}$$

and

$$P^2 \begin{pmatrix} x \\ y \\ z \end{pmatrix} = P \begin{pmatrix} x \\ y \\ 0 \end{pmatrix} = \begin{pmatrix} x \\ y \\ 0 \end{pmatrix};$$

therefore $P = P^2$, proving that P is indeed a projection.

Oblique projection

An example of a simple non-orthogonal (oblique) projection (for definition see below) is

$$P = \begin{bmatrix} 0 & 0 \\ \alpha & 1 \end{bmatrix};$$

It is easy to see that

$$P^2 = \begin{bmatrix} 0 & 0 \\ \alpha & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ \alpha & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ \alpha & 1 \end{bmatrix} = P.$$

proving that P is indeed a projection.

The projection P is orthogonal if and only if $\alpha = 0$.

http://en.wikipedia.org/wiki/Orthographic_projection

Orthographic projection
From Wikipedia, the free encyclopedia

Orthographic projection is a means of representing a three-dimensional object in two dimensions. It is a form of parallel projection, where the view direction is orthogonal to the projection plane, resulting in every plane of the scene appearing in affine transformation on the viewing surface. It is further divided into multiview orthographic projections and axonometric projections.

Orthographic projection corresponds to a perspective projection with a hypothetical viewpoint—e. g., one where the camera lies an infinite distance away from the object and has an infinite focal length, or "zooms".

Contents [hide]

- Multiview orthographic projections
- Pictorials
- See also
- References

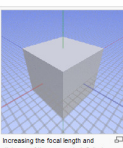
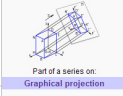
Multiview orthographic projections [edit]

With multiview orthographic projections, up to six pictures of an object are produced, with each projection plane parallel to one of the coordinate axes of the object. The views are positioned relative to each other according to either of two schemes: first-angle or third-angle projection. In each, the appearances of views may be thought of as being projected onto planes that form a 6-sided box around the object.

Pictorials [edit]

Main article: *Axonometric projection*

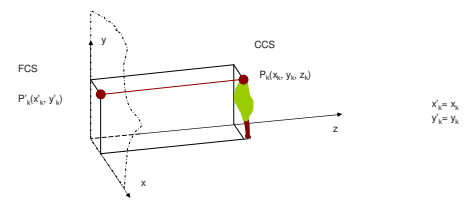
Within orthographic projection there is an ancillary category known as Pictorials. Pictorials show an image of an object as viewed from a skew direction in order to reveal all three directions (axes) of space.

Part of a series on: **Graphical projection**

Image Processing & Computer Graphics 14

Parallel projection



FCS $P_1(x_1, y_1)$

CCS $P_2(x_2, y_2, z_2)$

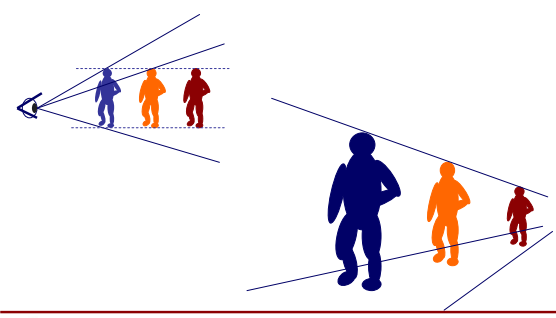
$x_2 = x_1$
 $y_2 = y_1$

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Image Processing & Computer Graphics 15

Principles of perspective projection

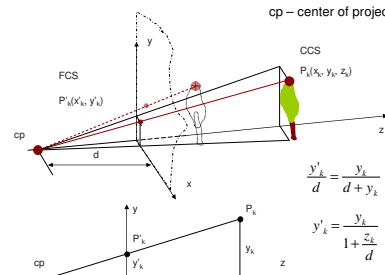


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Image Processing & Computer Graphics **16**

Perspective projection



cp – center of projection

FCS
 $P'_k(x'_k, y'_k)$

CCS
 $P_k(x_k, y_k, z_k)$

cp

d

x

y

z

$$\frac{y'_k}{d} = \frac{y_k}{d + y_k} \qquad \frac{x'_k}{d} = \frac{x_k}{d + z_k}$$

$y'_k = \frac{y_k}{1 + \frac{z_k}{d}}$ $x'_k = \frac{x_k}{1 + \frac{z_k}{d}}$

cp

d

y_k

x_k

z_k

What happens when d is huge?

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Wikipedia: affine transformation

Affine transformation

From Wikipedia, the free encyclopedia

This article includes a list of references or external links, but its sources remain unclear because it lacks inline citations. Please improve this article by introducing more precise citations where appropriate. *May 2008*

In geometry, an **affine transformation** or **affine map** or an **affinity** (from the Latin, *affinis*, "connected with") between two vector spaces (strictly speaking, two affine spaces) consists of a linear transformation followed by a translation:

$$x \mapsto Ax + b,$$

In the finite-dimensional case each affine transformation is given by a matrix A and a vector b , satisfying certain properties described below.

Geometrically, an affine transformation in Euclidean space is one that preserves

- The collinearity relation between points, i.e., three points which lie on a line continue to be collinear after the transformation
- Ratios of distances along a line, i.e., for distinct collinear points p_1, p_2, p_3 , the ratio $|p_2 - p_1| / |p_3 - p_2|$ is preserved

In general, an affine transformation is composed of linear transformations (rotation, scaling or shear) and a translation (or "shift"). Several linear transformations can be combined into a single one, so that the general formula given above is still applicable.

Contents [hide]

- Representation of affine transformations
- Properties of affine transformations
- Affine transformations and linear transformations
- Affine transformation of the plane
- Example of an affine transformation
- See also
- External links

Representation of affine transformations [edit]

Wikipedia: linear map

Linear map

From Wikipedia, the free encyclopedia

This article includes a list of references or external links, but its sources remain unclear because it lacks inline citations. Please improve this article by introducing more precise citations where appropriate. *June 2008*

In mathematics, a **linear map** (also called a **linear transformation**, **linear function** or **linear operator**) is a function between two vector spaces that preserves the operations of vector addition and scalar multiplication. The expression "linear operator" is in especially common use, for linear maps from a vector space to itself (endomorphisms). In advanced mathematics, the definition of linear function coincides with the definition of linear map.

In the language of abstract algebra, a linear map is a homomorphism of vector spaces, or a morphism in the category of vector spaces over a given field.

Contents [hide]

- Definition and first consequences
- Examples
- Matrices
- Examples of linear transformation matrices
- Forming new linear maps from given ones
- Endomorphisms and automorphisms
- Kernel, image and the rank-nullity theorem
- Algebraic classifications of linear transformations
- Continuity
- Applications
- See also
- References

Definition and first consequences [edit]

Examples of linear transformation matrices








Some special cases of linear transformations of two-dimensional space \mathbb{R}^2 are illuminating:

- rotation by 90 degrees clockwise:
 $A = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$
- rotation by θ degrees counterclockwise:
 $A = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix}$
- reflection against the x axis:
 $A = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
- scaling by 2 in all directions:
 $A = \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$
- vertical shear mapping:
 $A = \begin{bmatrix} 1 & m \\ 0 & 1 \end{bmatrix}$
- squeezing:
 $A = \begin{bmatrix} k & 0 \\ 0 & 1/k \end{bmatrix}$
- projection onto the y axis:
 $A = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$

Forming new linear maps from given ones

Linear transformation

Image Processing & Computer Graphics 20

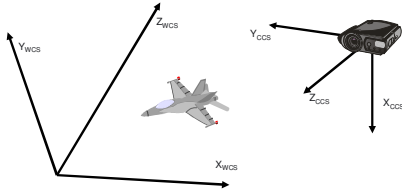
- Original image 
- Scaling 
- Rotation 
- Shear 
- Reflection 
- ?? 
- ?? 

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Affine transformation

Image Processing & Computer Graphics 21

- Let us transform co-ordinates in WCS onto CCS
- Affine transformation is a composition of translation and linear transformation
- Linear transformation is rotation, scaling, reflection and shear (usually only rotation is performed)



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Translation

$$\begin{bmatrix} x_k(TWCS) \\ y_k(TWCS) \\ z_k(TWCS) \end{bmatrix} = \begin{bmatrix} x_k(WCS) \\ y_k(WCS) \\ z_k(WCS) \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

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Linear transformation (Rotation matrix)

$$\begin{bmatrix} x_k(CCS) \\ y_k(CCS) \\ z_k(CCS) \end{bmatrix} = \begin{bmatrix} c_{xx} & c_{xy} & c_{xz} \\ c_{yx} & c_{yy} & c_{yz} \\ c_{zx} & c_{zy} & c_{zz} \end{bmatrix} \begin{bmatrix} x_k(WCS) \\ y_k(WCS) \\ z_k(WCS) \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

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Image Processing & Computer Graphics 24

Rotation matrix properties

- Rotation means no scaling, shear or reflection
- Properties:
 - Orthonormal
 - $|\det \mathbf{C}| = 1$ – no scaling
 - $\det \mathbf{C} > 0$ – no reflection
 - Orthogonal – no shear

$$\begin{bmatrix} x_k(CCS) \\ y_k(CCS) \\ z_k(CCS) \end{bmatrix} = \underbrace{\begin{bmatrix} c_{xx} & c_{xy} & c_{xz} \\ c_{yx} & c_{yy} & c_{yz} \\ c_{zx} & c_{zy} & c_{zz} \end{bmatrix}}_{\mathbf{C}} \begin{bmatrix} x_k(WCS) \\ y_k(WCS) \\ z_k(WCS) \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

$$\mathbf{C}^T \mathbf{C} = \mathbf{1}$$

$$\mathbf{C}^T \mathbf{C}^{-1} = \mathbf{1} \mathbf{C}^{-1}$$

$$\mathbf{C}^T = \mathbf{C}^{-1}$$


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Image Processing & Computer Graphics 25

Example 1

1. Camera is at $[a_x, a_y, a_z]^T$ in WCS,
2. Camera is directed along $[b_x, b_y, b_z]^T$ vector in WCS,
3. Camera stands straight (base is parallel to OYZ plane of WCS)

Find translation vector and rotation matrix


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Image Processing & Computer Graphics 26

Example 1

1. Camera is at $[a_x, a_y, a_z]^T$ in WCS. Therefore translation vector $[t_x, t_y, t_z]^T = -[a_x, a_y, a_z]^T$
2. Vector $[c_{zx}, c_{zy}, c_{zz}]^T$ transforms camera direction in WCS into Z-axis in CCS. Therefore it is equal to normalized camera direction.
 $[c_{zx}, c_{zy}, c_{zz}]^T = [b_x, b_y, b_z]^T / \|[b_x, b_y, b_z]^T\|$
3. Camera stands straight. Vector $[c_{zx}, c_{zy}, c_{zz}]^T$ is perpendicular $[c_{xx}, c_{xy}, c_{xz}]^T$ and parallel to Y axis and Z axis of WCS.
 $[c_{xx}, c_{xy}, c_{xz}]^T = [c_{zz}, 0, -c_{zy}]^T / \|[c_{zz}, 0, -c_{zy}]^T\|$
4. Vector $[c_{yx}, c_{yy}, c_{yz}]^T$ is parallel to $[c_{xx}, c_{xy}, c_{xz}]^T$ and $[c_{zx}, c_{zy}, c_{zz}]^T$. Therefore it is a vector product of the two.
 $[c_{yx}, c_{yy}, c_{yz}]^T = [c_{xx}, c_{xy}, c_{xz}]^T \times [c_{zx}, c_{zy}, c_{zz}]^T$

$$\begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

C_{xx}	C_{xy}	C_{xz}
C_{yx}	C_{yy}	C_{yz}
C_{zx}	C_{zy}	C_{zz}


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Image Processing & Computer Graphics 27

Example 2

1. Camera is at $[a_x, a_y, a_z]^T$ in WCS,
2. Camera is rotated by:
 - yaw α angle to the left
 - pitch β angle up
 - and rolled by γ angle counter clockwise

Find translation vector and rotation matrix


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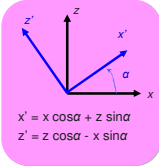
Image Processing & Computer Graphics 28

Example 2

1. $[t_x, t_y, t_z]^T = -[a_x, a_y, a_z]^T$

2. Rotation matrix is composed by three rotations
yaw, pitch and roll.

The three matrices are multiplied to produce a complete rotation in 3D space.



$x' = x \cos \alpha + z \sin \alpha$
 $z' = z \cos \alpha - x \sin \alpha$

$$C = \begin{bmatrix} \cos \gamma & \sin \gamma & 0 \\ -\sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \beta & -\sin \beta \\ 0 & \sin \beta & \cos \beta \end{bmatrix} \begin{bmatrix} \cos \alpha & 0 & \sin \alpha \\ 0 & 1 & 0 \\ -\sin \alpha & 0 & \cos \alpha \end{bmatrix}$$

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Image Processing & Computer Graphics 29

Example 2

$$\begin{bmatrix} x_k(\text{CCS}) \\ y_k(\text{CCS}) \\ z_k(\text{CCS}) \end{bmatrix} = \begin{bmatrix} \cos \gamma & \sin \gamma & 0 \\ -\sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \beta & -\sin \beta \\ 0 & \sin \beta & \cos \beta \end{bmatrix} \begin{bmatrix} \cos \alpha & 0 & \sin \alpha \\ 0 & 1 & 0 \\ -\sin \alpha & 0 & \cos \alpha \end{bmatrix} \begin{bmatrix} x_k(\text{WCS}) \\ y_k(\text{WCS}) \\ z_k(\text{WCS}) \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

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Image Processing & Computer Graphics 30

Homogeneous coordinates

Affine transformation is a composition of translation and linear transformation (summation of vectors and matrix multiplication).

$$\begin{bmatrix} x_k(\text{CCS}) \\ y_k(\text{CCS}) \\ z_k(\text{CCS}) \end{bmatrix} = \begin{bmatrix} c_{xx} & c_{xy} & c_{xz} \\ c_{yx} & c_{yy} & c_{yz} \\ c_{zx} & c_{zy} & c_{zz} \end{bmatrix} \begin{bmatrix} x_k(\text{WCS}) \\ y_k(\text{WCS}) \\ z_k(\text{WCS}) \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

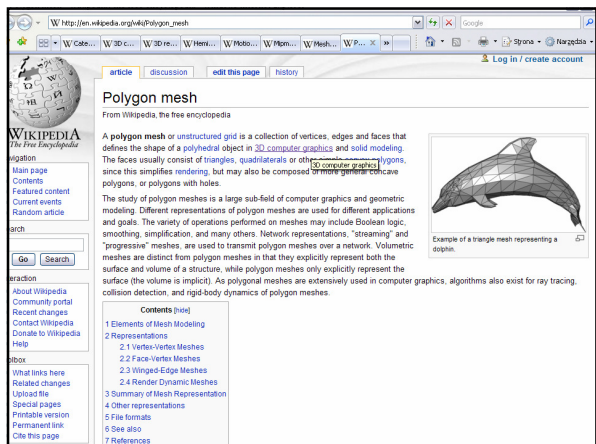
The affine transformation is represented by translation vector and rotation matrix.

However, the affine transformation can be represented just by a single matrix in homogeneous coordinates.

$$\begin{bmatrix} x_k(\text{CCS}) \\ y_k(\text{CCS}) \\ z_k(\text{CCS}) \\ 1 \end{bmatrix} = \begin{bmatrix} c_{xx} & c_{xy} & c_{xz} & 0 \\ c_{yx} & c_{yy} & c_{yz} & 0 \\ c_{zx} & c_{zy} & c_{zz} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_k(\text{WCS}) \\ y_k(\text{WCS}) \\ z_k(\text{WCS}) \\ 1 \end{bmatrix}$$

A 4x4 transformation matrix is often used in 3D graphics programs.

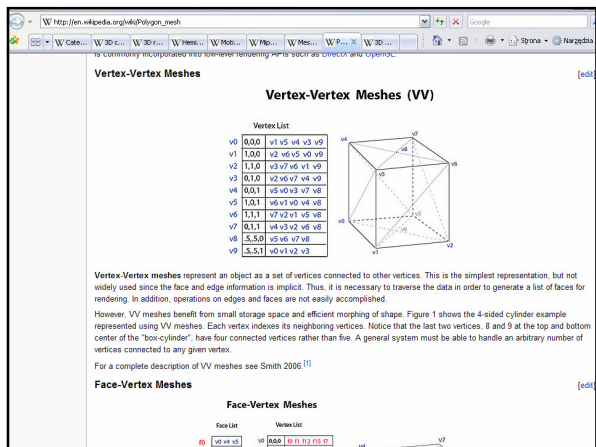
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The image shows a browser window displaying the Wikipedia page for 'Polygon mesh'. The page includes a search bar, navigation links, and a main content area with text and an image of a triangle mesh. A table of contents is visible on the left side of the page.

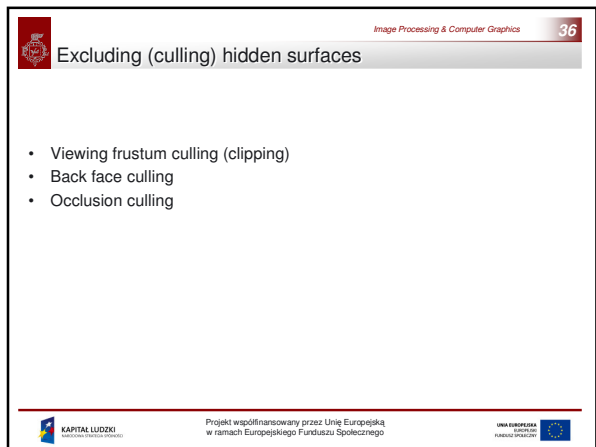
Contents (hide)

- 1 Elements of Mesh Modeling
- 2 Representations
 - 2.1 Vertex-Vertex Meshes
 - 2.2 Face-Vertex Meshes
 - 2.3 Winged-Edge Meshes
 - 2.4 Render Dynamic Meshes
- 3 Summary of Mesh Representation
- 4 Other representations
- 5 File formats
- 6 See also
- 7 References



The image shows a section of the Wikipedia article titled 'Vertex-Vertex Meshes (VV)'. It contains a table for the 'Vertex List' and a diagram of a mesh structure. Below the table, there is text explaining the representation and its limitations.

Vertex	x	y	z
v0	0.0,0	v1 v5 v4 v3 v9	
v1	1.0,0	v2 v6 v5 v0 v9	
v2	1.0,1	v3 v7 v6 v1 v9	
v3	0.0,1	v4 v8 v7 v0 v9	
v4	0.0,1	v5 v0 v2 v7 v8	
v5	1.0,1	v6 v1 v0 v4 v8	
v6	1.1,1	v7 v2 v1 v5 v8	
v7	0.1,1	v4 v3 v2 v5 v8	
v8	5.5,0	v5 v6 v7 v8	
v9	5.5,1	v0 v1 v2 v3	



The slide is titled 'Excluding (culling) hidden surfaces' and is part of a presentation on 'Image Processing & Computer Graphics'. It lists three types of culling: Viewing frustum culling (clipping), Back face culling, and Occlusion culling. The slide also features logos for 'KAPITAL LUDZKI' and the European Union.

- Viewing frustum culling (clipping)
- Back face culling
- Occlusion culling

Wikipedia article: **Hidden surface determination**

In 3D computer graphics, **hidden surface determination** (also known as **Hidden Surface Removal (HSR)**, or **Visible Surface Determination (VSD)**) is the process used to determine which surfaces and parts of surfaces are not visible from a certain viewpoint. A hidden surface determination algorithm is a solution to the **visibility problem**, which was one of the first major problems in the field of 3D computer graphics. The process of hidden surface determination is sometimes called **hiding**, and such an algorithm is sometimes called a **hider**. The analogue for line rendering is **hidden line removal**. Hidden surface determination is necessary to render an image correctly, so that one cannot look through walls in virtual reality, for example.

There are many techniques for hidden surface determination. They are fundamentally an exercise in sorting, and usually vary in the order in which the sort is performed and how the problem is subdivided. Sorting large quantities of graphics primitives is usually done by divide and conquer.

Contexts (pick)

- 1 Hidden surface removal algorithms
- 2 Culling and VSD
- 2.1 Viewing frustum culling
- 2.2 Backface culling
- 2.3 Contribution culling
- 2.4 Occlusion culling
- 3 Divide and conquer

Hidden surface removal algorithms [edit]

Considering the rendering pipeline, the projection, the clipping, and the rasterization steps are handled differently by the following algorithms:

- **Z-buffering** During rasterization the depthZ value of each pixel (or sample in the case of anti-aliasing, but without loss of generality we use the term *pixel*) is checked against an existing depth value. If the current pixel is behind the pixel in the Z-buffer, the pixel is rejected, otherwise it is shaded and its depth value replaces the one in the Z-buffer. Z-buffering supports dynamic scenes easily, and is currently implemented efficiently in graphics hardware. This is the current standard. The cost of using Z-buffering is that it uses up

Wikipedia article: **Culling and VSD**

A related area to VSD is culling, which usually happens before VSD in a rendering pipeline. Primitives or batches of primitives can be rejected in their entirety, which usually reduces the load on a well-designed system. The advantage of culling early on the pipeline is that entire objects that are invisible do not have to be fetched, transformed, rasterized or shaded. Here are some types of culling algorithms:

Viewing frustum culling [edit]

The viewing frustum is a geometric representation of the volume visible to the virtual camera. Naturally, objects outside this volume will not be visible in the final image, so they are discarded. Often, objects lie on the boundary of the viewing frustum. These objects are cut into pieces along this boundary in a process called **clipping**, and the pieces that lie outside the frustum are discarded as there is no place to draw them.

Backface culling [edit]

Since meshes are hollow shells, not solid objects, the back side of some faces, or polygons, in the mesh will never face the camera. Typically, there is no reason to draw such faces. This is responsible for the effect often seen in computer and video games in which, if the camera happens to be inside a mesh, rather than seeing the "inside" surfaces of the mesh, it mostly disappears. (Some game engines continue to render any forward-facing or double-sided polygons, resulting in stray shapes appearing without the rest of the generated mesh.)

Contribution culling [edit]

Often, objects are so far away that they do not contribute significantly to the final image. These objects are thrown away if their screen projection is too small. See **Clipping plane**.

Occlusion culling [edit]

Objects that are entirely behind other opaque objects may be culled. This is a very popular mechanism to speed up the rendering of large scenes that have a moderate to high depth complexity. There are several types of occlusion culling approaches:

- **Potentially visible set** or **PVS** rendering, divides a scene into regions and pre-computes visibility for them. These visibility sets are then indexed at run-time to obtain high quality visibility sets (accounting for complex occluder interactions) quickly.
- **Portal rendering** divides a scene into cells/sectors (rooms) and portals (doors), and computes which sectors are visible by clipping them against portals.

Hansong Zhang's dissertation "Effective Occlusion Culling for the Interactive Display of Arbitrary Models" describes an occlusion culling

Image Processing & Computer Graphics 39

Viewing frustum culling

If the screen is $W \times H$, and the far plane is at distance D from the near plane then the visible will be point P_k of CCS coordinates:

$$0 \leq z_k \leq D \quad -\frac{W}{2} \left(1 + \frac{z_k}{d}\right) \leq x_k \leq \frac{W}{2} \left(1 + \frac{z_k}{d}\right) \quad -\frac{H}{2} \left(1 + \frac{z_k}{d}\right) \leq y_k \leq \frac{H}{2} \left(1 + \frac{z_k}{d}\right)$$

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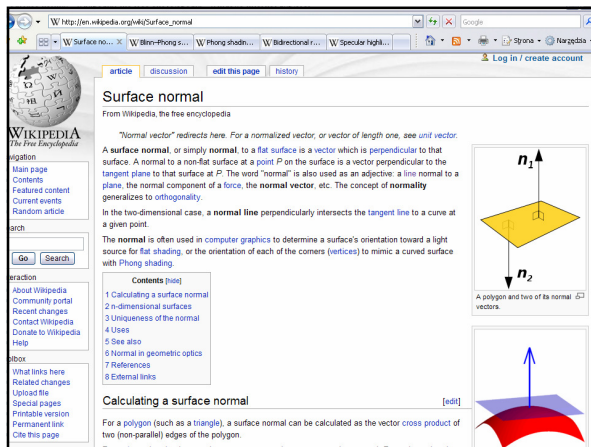
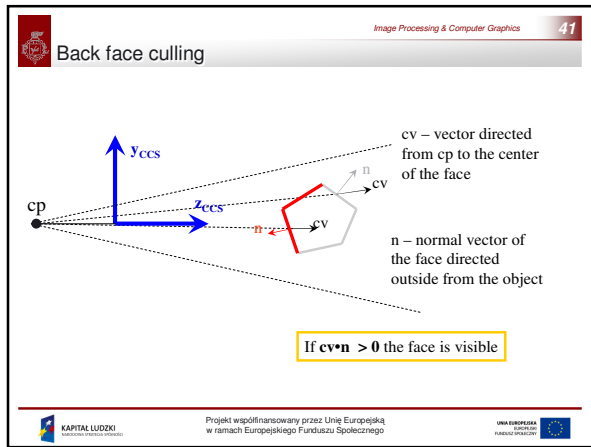


Image Processing & Computer Graphics 43

Normal vectors

If the face is

1. coplanar and convex
2. vertices are listed in clockwise order, when looking from the inside of the object

then:

$$n = (p_2 p_3 \times p_2 p_1) / \| p_2 p_3 \times p_2 p_1 \|$$

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Image Processing & Computer Graphics 44

Occlusions

The closer object occludes the farther one.

- **Z-buffer (or depth buffer)**– a image size matrix for storage distance information for projected points (pixels). When image is rendered the Z-buffer is filled with distances for pixels being draw. Pixel is redraw only when distance to projected point is closer then a distance stored in Z-buffer.

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Wikipedia article: Z-buffering

In computer graphics, **z-buffering** is the management of image depth coordinates in three-dimensional (3-D) graphics, usually done in hardware, sometimes in software. It is one solution to the visibility problem, which is the problem of deciding which elements of a rendered scene are visible, and which are hidden. The painter's algorithm is another common solution which, though less efficient, can also handle non-opaque scene elements. Z-buffering is also known as **depth buffering**.

When an object is rendered by a 3D graphics card, the depth of a generated pixel (z coordinate) is stored in a buffer (the z-buffer or depth buffer). This buffer is usually arranged as a two-dimensional array (x,y) with one element for each screen pixel. If another object of the scene must be rendered in the same pixel, the graphics card compares the two depths and chooses the one closer to the observer. The chosen depth is then saved to the z-buffer, replacing the old one. In the end, the z-buffer will allow the graphics card to correctly reproduce the usual depth perception: a close object hides a farther one. This is called **z-culling**.

The granularity of a z-buffer has a great influence on the scene quality: a 16-bit z-buffer can result in artifacts (called "z-fighting") when two objects are very close to each other. A 24-bit or 32-bit z-buffer behaves much better, although the problem cannot be entirely eliminated without additional algorithms. An 8-bit z-buffer is almost never used since it has too little precision.

Contents [hide]

- 1 Uses
- 2 Developments
- 3 Z-culling
- 4 Mathematics
- 4.1 W-buffer
- 5 References
- 6 See also
- 7 External links

Image Processing & Computer Graphics 46

Light and shading

- Light sources
- Shading models
- Object interactions

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Image Processing & Computer Graphics 47

Light source

- Ambient light
- Directed light
- Point light source

• Light color (RGB model)

R=0
G=1
B=0

R=1
G=0
B=1

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Image Processing & Computer Graphics 48

Modele odbić

Ambient illumination

Flat shading

Gouraud model (soft transitions)

Phong model (specular light)

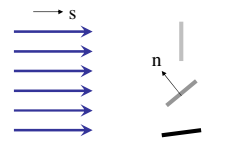
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Image Processing & Computer Graphics 49

Shading models (flat shading)

- Directed light
- Face is uniform
- s is a normalized light vector
- n is a face normal vector
- $L_R L_G L_B$ are color light components
- $J_R J_G J_B$ are color components of face surface
- Face color is given the following equation:



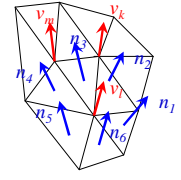
$$\begin{bmatrix} L_R J_R \\ L_G J_G \\ L_B J_B \end{bmatrix} n \cdot s$$

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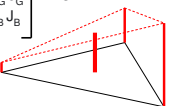
Image Processing & Computer Graphics 50

Gouraud shading model

- Normal vectors at vertices are estimated as average of normal vectors of connected faces
- Vector n' is interpolated over the face area by means of bilinear interpolation
- Face color may vary over the face area



$$V_i = (n_1 + n_2 + \dots + n_i) / i$$

$$\begin{bmatrix} L_R J_R \\ L_G J_G \\ L_B J_B \end{bmatrix} n' \cdot s$$


- Triangular mesh
- Directed light or point source light

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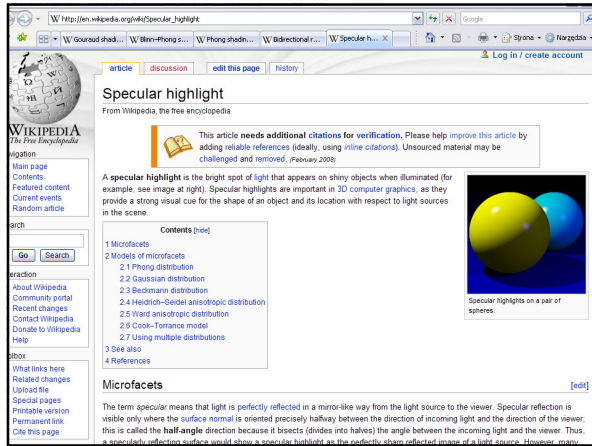
The screenshot shows the Wikipedia page for 'Gouraud shading'. The article text includes:

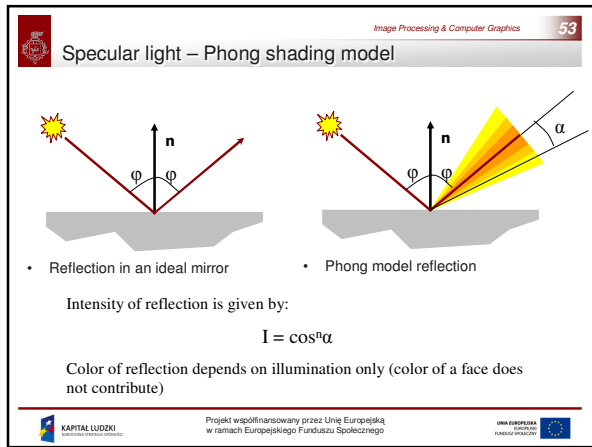
Gouraud shading, named after Henri Gouraud, is a method used in computer graphics to simulate the differing effects of light and colour across the surface of an object. In practice, Gouraud shading is used to achieve smooth lighting on low-polygon surfaces without the heavy computational requirements of calculating lighting for each pixel. Gouraud first published the technique in 1971.

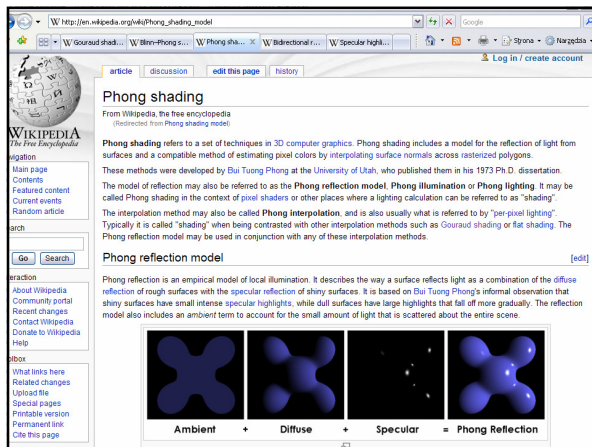
Principles behind the method

The basic principle behind the method is as follows. An estimate to the surface normal of each vertex in a 3D model is found by averaging the surface normals of polygons which meet at each vertex. Using these estimates, lighting computations based on the Phong reflection model are then performed to produce colour intensities at the vertices. Screen pixel intensities can then be bilinearly interpolated from the colour values calculated at the vertices. In a simpler sense, a gradient is formed in the area where the vertices meet.

Gouraud shading's strength and weakness lies in its interpolation. Interpolating colour values from three samples of expensive lighting calculations is much less processor intensive than performing that lighting calculation for each pixel, as is done in Phong shading. However, highly localized lighting effects (such as specular highlights, e.g. the glint of reflected light on the surface of an apple) will not be rendered correctly, and if a highlight lies in the middle of a polygon, but does not spread to the polygon's vertex, it will not be apparent in a Gouraud rendering; conversely, if a highlight occurs at the vertex of a polygon, it will be rendered correctly at this vertex (as this is where the lighting model is applied), but will be spread unnaturally across all neighboring polygons via the interpolation method. The problem is easily spotted in a rendering which ought to have a specular highlight moving smoothly across the surface of a model as it rotates. Gouraud shading will instead produce a highlight continuously fading in and out across neighboring portions of the model, peaking in intensity when the intended specular highlight passes over a vertex of the model. (This can be improved by increasing the







http://en.wikipedia.org/wiki/Blinn-Phong_shading_model

article discussion edit this page history

Blinn-Phong shading model

From Wikipedia, the free encyclopedia

The **Blinn-Phong shading model** (also called **Blinn-Phong reflection model** or **modified Phong reflection model**) is a modification to the Phong reflection model developed by Jim Blinn.^[1]

Blinn-Phong is the default shading model used in OpenGL and DirectX3D's fixed-function pipeline (before DirectX 10), and is carried out on each vertex as it passes down the graphics pipeline; pixel values between vertices are interpolated by Gouraud shading by default, rather than the more expensive Phong shading.

Contents (hide)

- 1 The concept
- 2 Efficiency
- 3 References
- 4 See also

The concept [edit]

In Phong shading one must continually recalculate the angle $R \cdot V$ between a viewer (V) and the beam from a light-source (L) reflected (R) on a surface.

If we instead calculate a halfway vector between the viewer and light-source vectors,

$$H = \frac{L + V}{|L + V|}$$

we can replace $R \cdot V$ with $N \cdot H$, where N is the normalized surface normal.

This dot product represents the cosine of an angle that is half of the angle represented by Phong's dot product, if V , L , N and H all lie in the same plane. The angle between N and H is therefore sometimes called the halfway angle.

The halfway angle is smaller than the angle we want in Phong's model, but considering that Phong is using $(R \cdot V)^q$, we can set an exponent q' so that $(N \cdot H)^{q'}$ is closer to the former expression. The size of the specular highlights can be matched in this way

http://en.wikipedia.org/wiki/Bidirectional_reflectance_distribution_function

article discussion edit this page history

Bidirectional reflectance distribution function

From Wikipedia, the free encyclopedia

The **bidirectional reflectance distribution function** (BRDF, $f_r(\omega_i, \omega_o)$) is a 4-dimensional function that defines how light is reflected at an opaque surface. The function takes an incoming light direction, ω_i , and outgoing direction, ω_o , both defined with respect to the surface normal N , and returns the ratio of reflected radiance exiting along ω_o to the irradiance incident on the surface from direction ω_i . Note that each direction ω is itself parameterized by azimuth angle θ and elevation ϕ , therefore the BRDF as a whole is 4-dimensional. The BRDF has units sr^{-1} , with steradians (sr) being a unit of solid angle.

Contents (hide)

- 1 Definition
- 2 Physically based BRDFs
- 3 Applications
- 4 Models
- 4.1 Some examples
- 5 Acquisition
- 6 See also
- 7 Further reading
- 8 References

Definition [edit]

The BRDF was first defined by Edward Nicodemus in the mid-sixties^[1]. The modern definition is:

$$f_r(\omega_i, \omega_o) = \frac{dL_o(\omega_o)}{dE_i(\omega_i)} = \frac{dL_r(\omega_o)}{I_i(\omega_i) \cos(\theta_i) d\omega_i}$$

where E is the irradiance, L is the radiance, and θ is the angle made between ω and the surface normal.

Image Processing & Computer Graphics **57**

Textures

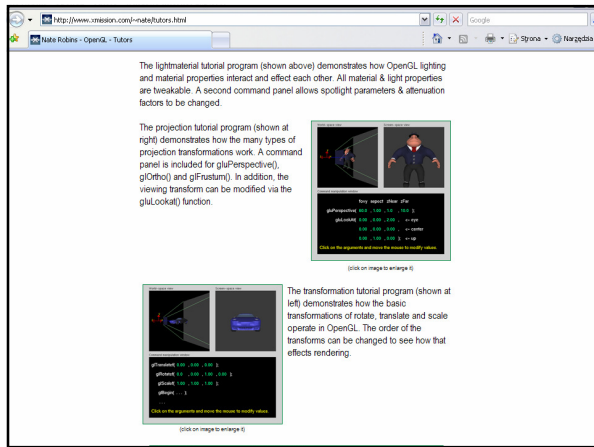
Texture allows to model details of a surface of real objects (e.g. sandstone, bricks, wood, etc.). Texture is defined in the form of 2D raster image. Texture is projected on the object face (pixels of the face drawn on the film plane sample texture)

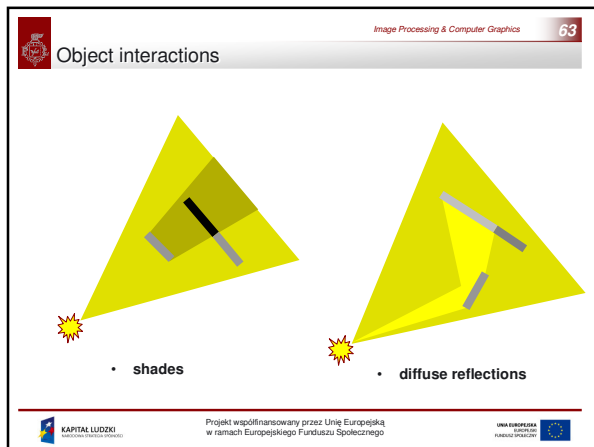
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Models of reflection/scattering and shading are used to describe the appearance of a surface. Although these issues may seem like problems all on their own, they are studied almost exclusively within the context of rendering. Modern 3D computer graphics rely heavily on a simplified reflection model called *Phong reflection model* (not to be confused with Phong shading). In refraction of light, an important concept is the *refractive index*. In most 3D programming implementations, the term for this value is "index of refraction," usually abbreviated "IOR."

- **Reflection/Scattering** - How light interacts with the surface at a given point
- **Shading** - How material properties vary across the surface

Reflection [edit]

Reflection or scattering is the relationship between incoming and outgoing illumination at a given point. Descriptions of scattering are usually given in terms of a bidirectional scattering distribution function or BSDF. Popular reflection rendering techniques in 3D computer graphics include:

- **Flat shading**: A technique that shades each polygon of an object based on the polygon's "normal" and the position and intensity of a light source.
- **Gouraud shading**: Invented by H. Gouraud in 1971, a fast and resource-conscious vertex shading technique used to simulate smoothly shaded surfaces.
- **Texture mapping**: A technique for simulating a large amount of surface detail by mapping images (textures) onto polygons.
- **Phong shading**: Invented by Bui Tuong Phong, used to simulate specular highlights and smooth shaded surfaces.
- **Bump mapping**: Invented by Jim Blinn, a normal-perturbation technique used to simulate wrinkled surfaces.
- **Cell shading**: A technique used to imitate the look of hand-drawn animation.

Shading [edit]

Shading addresses how different types of scattering are distributed across the surface (i.e., which scattering function applies where). Descriptions of this kind are typically expressed with a program called a *shader*. (Note that there is some confusion since the word "shader" is sometimes used for programs that describe local geometric variation.) A simple example of shading is texture mapping, which uses an image to specify the diffuse color at each point on a surface, giving it more apparent detail.

Transport [edit]



Transport [edit]

Transport describes how illumination in a scene gets from one place to another. *Visibility* is a major component of light transport.

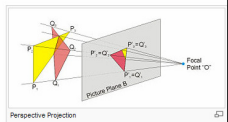
Projection [edit]

The shaded three-dimensional objects must be flattened so that the display device - namely a monitor - can display it in only two dimensions, this process is called *3D projection*. This is done using projection and, for most applications, *perspective projection*. The basic idea behind perspective projection is that objects that are further away are made smaller in relation to those that are closer to the eye. Programs produce perspective by multiplying a dilation constant raised to the power of the negative of the distance from the observer. A dilation constant of one means that there is no perspective. High dilation constants can cause a "fish-eye" effect in which image distortion begins to occur. Orthographic projection is used mainly in CAD or CAM applications where scientific modeling requires precise measurements and preservation of the third dimension.

See also [edit]

- Ambient occlusion
- Computer vision
- Geometry pipeline
- Geometry processing
- Graphics
- Graphics processing unit (GPU)
- Graphical output devices
- Image processing
- Painter's algorithm
- Reflection (computer graphics)
- Rendering (computer graphics)
- SIGGRAPH

External links [edit]



Ray tracing (graphics)

From Wikipedia, the free encyclopedia

This article needs additional citations for verification. Please help improve this article by adding reliable references (ideally, using inline citations). Unsourced material may be challenged and removed. *March 2008*

In computer graphics, **ray tracing** is a technique for generating an image by tracing the path of light through pixels in an image plane. The technique is capable of producing a very high degree of photorealism, usually higher than that of typical scanline rendering methods, but at a greater computational cost. This makes ray tracing best suited for applications where the image can be rendered slowly ahead of time, such as in still images and film and television special effects, and more poorly suited for real-time applications like computer games where speed is critical. Ray tracing is capable of simulating a wide variety of optical effects, such as reflection and refraction, scattering, and chromatic aberration.

Contents [hide]

- Algorithm overview
- Detailed description of ray tracing computer algorithm and its genesis
 - What happens in nature
 - Ray casting algorithm
 - Ray tracing algorithm
 - Advantages over other rendering methods
 - Disadvantages
 - Reversed direction of traversal of scene by the rays
 - Algorithm, classical recursive ray tracing
- In real time
- Example
- See also
- Software
 - References



Wikipedia:en:Ray tracing

Algorithm overview

Optical ray tracing describes a method for producing visual images constructed in 3D computer graphics environments, with more photorealism than either ray casting or scanline rendering techniques. It works by tracing a path from an imaginary eye through each pixel in a virtual screen, and calculating the color of the object visible through it.

Scenes in raytracing are described mathematically by a programmer or by a visual artist (typically using intermediary tools). Scenes may also incorporate data from images and models captured by means such as digital photography.

Typically, each ray must be tested for intersection with some subset of all the objects in the scene. Once the nearest object has been identified, the algorithm will estimate the incoming light at the point of intersection, examine the material properties of the object, and combine this information to calculate the final color of the pixel. Certain illumination algorithms and reflective or translucent materials may require more rays to be re-cast into the scene.

It may at first seem counterintuitive or "backwards" to send rays away from the camera, rather than into it (as actual light does in reality), but doing so is in fact many orders of magnitude more efficient. Since the overwhelming majority of light rays from a given light source do not make it directly into the viewer's eye, a "forward" simulation could potentially waste a tremendous amount of computation on light paths that are never recorded. A computer simulation that starts by casting rays from the light source is called Photon mapping, and it takes much longer than a comparable ray trace.

Therefore, the shortcut taken in raytracing is to presuppose that a given ray intersects the view frame. After either a maximum number of reflections or a ray traveling a certain distance without intersection, the ray ceases to travel and the pixel's value is updated. The light intensity of this pixel is computed using a number of algorithms, which may include the classic rendering algorithm and may also incorporate techniques such as radiosity.

Detailed description of ray tracing computer algorithm and its genesis

What happens in nature

Wikipedia:en:Ray casting

Ray casting

From Wikipedia, the free encyclopedia

Ray casting is the use of ray-surface intersection tests to solve a variety of problems in computer graphics. The term was first used in computer graphics in a 1982 paper by Scott Roth to describe a method for rendering CSG models.^[1]

Usage

- the general problem of determining the first object intersected by a ray,^[2]
- a technique for hidden surface removal based on finding the first intersection of a ray cast from the eye through each pixel of an image,
- a non-recursive variant of ray tracing that only casts primary rays, or
- a direct volume rendering method, also called volume ray casting.

Although "ray casting" and "ray tracing" were often used interchangeably in early computer graphics literature^[3], more recent usage tries to distinguish the two.^[4]

Concept

Ray casting is not a synonym for ray tracing, but can be thought of as an abridged, and significantly faster, version of the ray tracing algorithm. Both are image order algorithms used in computer graphics to render three dimensional scenes to two dimensional screens by following rays of light from the eye of the observer to a light source. Ray casting does not compute the new tangents a ray of light might take after intersecting a surface on its way from the eye to the source of light. This eliminates the possibility of accurately rendering reflections, refractions, or the natural fall off of shadows – however all of these elements can be faked to a degree, by creative use of texture maps or other methods. The high speed of calculation made ray casting a handy rendering method in early real-time 3D video games.

In nature, a light source emits a ray of light which travels, eventually, to a surface that interrupts its progress. One can think of this "ray" as a stream of photons traveling along the same path. At this point, any combination of three things might happen with this light ray: absorption, reflection, and refraction. The surface may reflect all or part of the light ray, in one or more directions. It might also absorb part of the light ray, resulting in a loss of intensity of the reflected and/or refracted light. If the surface has any transparent or translucent properties, it refracts a portion of the light beam into itself in a different direction while absorbing some (or all) of the spectrum (and possibly altering the color). Between absorption, reflection, and refraction, all of the incoming light must be accounted for, and no more. A surface cannot, for instance, reflect 66% of an incoming light ray, and refract 50%, since the two would add up to be 116%. From here, the reflected and/or refracted rays may strike other surfaces, where their absorptive, refractive, and reflective properties are again calculated based on the incoming rays. Some of these rays travel in such a way that they hit our eye, causing us to see the scene and so contribute to the final rendered image.

Attempting to simulate this real-world process of tracing light rays using a computer can be considered extremely wasteful, as only a minuscule fraction of the rays in a scene would actually reach the eye.

The first ray casting (versus ray tracing) algorithm used for rendering was presented by Arthur Appel in 1968.^[5] The idea behind ray casting is to shoot rays from the eye, one per pixel, and find the closest object blocking the path of that ray - think of an image as a screen-door, with each square in the screen being a pixel. This is then the object the eye normally sees through that pixel. Using the material properties and the effect of the lights in the scene, this algorithm can determine the shading of this object. The simplifying assumption is made that if a surface faces a light, the light will reach that surface and not be blocked or in shadow. The shading of the surface is computed using traditional 3D computer graphics shading models. One important advantage ray casting offered over older scanline algorithms is its ability to easily deal with non-planar surfaces and solids, such as cones and spheres. If a mathematical surface can be intersected by a ray, it can be rendered using ray casting. Elaborate objects can be created by using solid modelling techniques and easily rendered.

Ray casting for producing computer graphics was first used by scientists at Mathematical Applications Group, Inc. (MAGI) of Elmsford, New York. New York^[citation needed]. In 1966 the company was created to perform radiation exposure calculations for the Department of Defense. MAGI's software calculated not only how the gamma rays bounced off surfaces (ray casting for radiation had been done since the 1940s), but also how they penetrated and reflected within. These studies helped the government to determine certain military applications: constructing military vehicles that would protect troops from radiation, designing re-entry vehicles for space exploration. Under the direction of Dr. Philip

Wikipedia:en:Ray casting

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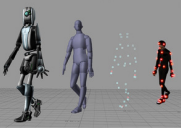
http://en.wikipedia.org/wiki/Motion_capture

Optical: Active marker [edit]

Active optical systems triangulate positions by illuminating one LED at a time very quickly or multiple LEDs with software to identify them by their relative positions, somewhat akin to celestial navigation. Rather than reflecting light back that is generated externally, the markers themselves are powered to emit their own light. Since Inverse Square law provides 1/4 the power at 2 times the distance, this can increase the distances and volume for capture. LM used active Markers in Van Helming to allow capture of the Hargraves on very large sets. The power to each marker can be provided sequentially in phase with the capture system providing a unique identification of each marker for a given capture frame at a cost to the resultant frame rate. The ability to identify each marker in this manner is useful in realtime applications. The alternative method of identifying markers is to do it algorithmically requiring extra processing of the data.

Optical: Time modulated active marker [edit]

Active marker systems can further be refined by strobing one marker on at a time, or tracking multiple markers over time and modulating the amplitude or pulse width to provide marker ID. 12 megapixel spatial resolution modulated systems show more subtle movements than 4 megapixel optical systems by having both higher spatial and temporal resolution. Directors can see the actors performance in real time, and watch the results on the mocap driven CG character. The unique marker IDs reduce the turnaround, by eliminating marker swapping and providing much cleaner data than other technologies. LEDs with onboard processing and a radio synchronization allow motion capture outdoors in direct sunlight, while capturing at 490 frames per second due to a high speed electronic shutter. Computer processing of modulated IDs allows less hand cleanup or filtered results for lesser operational costs. This higher accuracy and resolution requires more processing than passive technologies, but the additional processing is done at the camera to improve resolution via a subpixel or centroid processing, providing both high resolution and high speed. These motion capture systems are typically under \$50,000 for an eight camera, 12 megapixel spatial resolution 480 hertz system with one actor.



A high-resolution active marker system with 3,600 × 3,600 resolution at 480 hertz providing real-time submillimeter positions.

Optical: Semi-passive Imperceptible Marker [edit]

One can reverse the traditional approach based on high speed cameras. Systems such as Prakash use inexpensive multi-LED high speed projectors. The specially built multi-LED IR projectors optically encode the space. Instead of retro-reflective or active light emitting diode (LED) markers, the system uses photosensitive marker tags to decode the optical signals. By attaching tags with photo sensors to scene




Image Processing & Computer Graphics 80

Summary, discussion and quiz

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