

KAPITAŁ LUDZKI
NARODOWA STRATEGIA SPÓJNOŚCI

UNIA EUROPEJSKA
EUROPEJSKI FUNDUSZ SPOŁECZNY

„Image Processing and Computer Graphics”

Prezentacja multimedialna współfinansowana przez Unię Europejską w ramach Europejskiego Funduszu Społecznego w projekcie pt. „Innowacyjna dydaktyka bez ograniczeń - zintegrowany rozwój Politechniki Łódzkiej - zarządzanie Uczelnią, nowoczesna oferta edukacyjna i wzmacniania zdolności do zatrudniania osób niepełnosprawnych”

Politechnika Łódzka, ul. Żeromskiego 116, 90-924 Łódź, tel. (042) 631 28 83
www.kapitalludzki.p.lodz.pl

Contribution Image Processing & Computer Graphics 2

Lecturer:
Piotr M. Szczypiński, Dr inż.
Institute of Electronics, Technical University of Lodz
Wolczanska 211/215, 90-924 Lodz, Poland
tel. +48426312638
<http://www.elel.p.lodz.pl/pms>
pms@p.lodz.pl

Fragments of the lecture were also provided by
Andrzej Materka, Michał Strzelecki, Paweł Strumiłło,
Piotr Romaniuk, Piotr Makowski
and were used with permission.

Portions of this lecture are illustrated with articles from the wikipedia
(GNU Free Documentation License
http://en.wikipedia.org/wiki/Wikipedia:Text_of_the_GNU_Free_Documentation_License)

Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego

Image & video data compression Image Processing & Computer Graphics 3

- Image compression motivation
- Lossless vs. lossy compression (Information redundancy & Psychovisual redundancy)
- Lossless compression – selected methods
 - Run-length encoding
 - Huffman coding
 - Delta encoding
 - Deflate & LZW
- Lossy compression – selected methods (*Quid pro quo*)
 - Transform methods (Fourier, Cosine, Wavelet transforms)
 - Subsampling (chroma subsampling)
 - Posterization and paletted images
- Image compression applications: JPEG, JPEG 2000
- Video compression applications: MPEG1, MPEG2, MPEG4
- Compression in medical imaging

Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego

Image Processing & Computer Graphics **4**

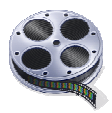
Need for image compression

Standard definition TV PAL image:
576 lines x 720 rows x 3 B = 1.2 MB


Frames in 2-hour video:
25 fps x 7200 s = 180 000 frames

Capacity of video file: 180 000 frames x 1.2 MB = 210 GB

DVD:
4.7 GB



Compress data 44x !



Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego

Wikipedia - http://en.wikipedia.org/wiki/Data_compression

Data compression

From Wikipedia, the free encyclopedia

"Source coding" redirects here. For the term in computer programming, see Source code.

In computer science and information theory, **data compression** or **source coding** is the process of encoding information using fewer bits (or other information-bearing units) than an **unencoded** representation would use through use of specific encoding schemes. As with any communication, compressed data communication only works when both the sender and receiver of the information understand the encoding scheme. For example, this text makes sense only if the receiver understands that it is intended to be interpreted as characters representing the English language. Similarly, compressed data can only be understood if the decoding method is known by the receiver.

Compression is useful because it helps reduce the consumption of expensive resources, such as hard disk space or transmission bandwidth. On the downside, compressed data must be decompressed to be used, and this extra processing may be detrimental to some applications. For instance, a compression scheme for video may require expensive hardware for the video to be decompressed fast enough to be viewed as it's being decompressed (the option of decompressing the video in full before watching it may be inconvenient, and requires storage space for the decompressed video). The design of data compression schemes therefore involves trade-offs among various factors, including the degree of compression, the amount of distortion introduced (if using a lossy compression scheme), and the computational resources required to compress and uncompress the data.

Contents

- Lossless versus lossy compression
- Applications
- Theory
- See also
 - 4.1 Data compression topics
 - 4.2 Compression algorithms
 - 4.2.1 Lossless data compression
 - 4.2.2 Lossy data compression
 - 4.2.3 Example implementations
 - 4.3 Copora

Wikipedia - http://en.wikipedia.org/wiki/Image_compression

Image compression

From Wikipedia, the free encyclopedia

Image compression is the application of Data compression on digital images. In effect, the objective is to reduce redundancy of the image data in order to be able to store or transmit data in an efficient form.

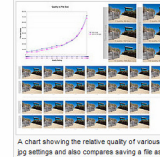
Image compression can be lossy or lossless. Lossless compression is sometimes preferred for artificial images such as technical drawings, icons or comics. This is because lossy compression methods, especially when used at low bit rates, introduce compression artifacts. Lossless compression methods may also be preferred for high value content, such as medical imagery or image scans made for archival purposes. Lossy methods are especially suitable for natural images such as photos in applications where minor (sometimes imperceptible) loss of fidelity is acceptable to achieve a substantial reduction in bit rate. The lossy compression that produces imperceptible differences can be called *visually lossless*.

Methods for lossless image compression are:

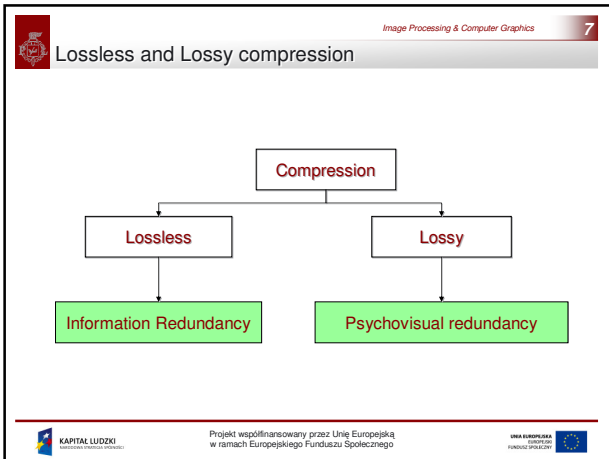
- Run-length encoding – used as default method in PCX and as one of possible in BMP, TGA, TIFF
- DPCM and Predictive Coding
- Entropy encoding
- Adaptive dictionary algorithms such as LZW – used in GIF and TIFF
- Deflation – used in PNG, MNG and TIFF

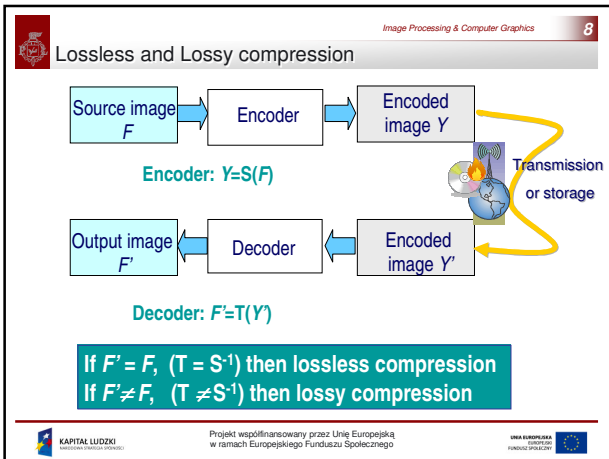
Methods for lossy compression:

- Reducing the color space to the most common colors in the image. The selected colors are specified in the color palette in the header of the compressed image. Each pixel just references the index of a color in the color palette. This method can be combined with dithering to avoid posterization.
- Chroma subsampling. This takes advantage of the fact that the eye perceives spatial changes of brightness more sharply than those of color, by averaging or dropping some of the chrominance information in the image.
- Transform coding. This is the most commonly used method. A Fourier-related transform such as DCT or the wavelet transform are



A chart showing the relative quality of various jpg settings and also compares saving a file as a jpg normally and using a "save for web" technique.





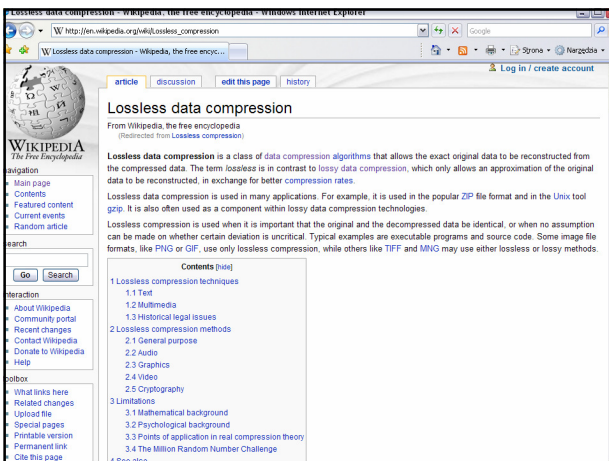



Image Processing & Computer Graphics 10

Source entropy

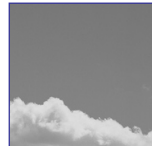
Source *entropy*:

$$E_F = - \sum_{i=0}^{L-1} p(l_i) \log_2 p(l_i)$$

represents the average information per source output.
 For data source given in the form of an image, $p(l_i)$ – is the probability of occurrence of gray level l_i .
Entropy can be interpreted as the average number of bits required for coding a single image pixel.



E = 7.01



E = 5.31

Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego

Entropy (information theory) - Wikipedia, the free encyclopedia - Windows Internet Explorer

http://en.wikipedia.org/wiki/Entropy_(information_theory)

article | discussion | edit this page | history

Entropy (information theory)

From Wikipedia, the free encyclopedia
 (Redirected from Entropy (information theory))

This article is about the Shannon entropy in *information theory*. For other uses, see *Entropy (disambiguation)*.

In *information theory*, **entropy** is a measure of the uncertainty associated with a random variable. The term by itself in this context usually refers to the **Shannon entropy**, which quantifies, in the sense of an expected value, the information contained in a message, usually in units such as bits. Equivalently, the Shannon entropy is a measure of the average information content one is missing when one does not know the value of the random variable. The concept was introduced by Claude E. Shannon in his 1948 paper "A Mathematical Theory of Communication".

Shannon's entropy represents an absolute limit on the best possible *lossless* compression of any communication, under certain constraints: treating messages to be encoded as a sequence of independent and identically-distributed random variables, Shannon's source coding theorem shows that, in the limit, the average length of the shortest possible representation to encode the messages in a given alphabet is their entropy divided by the logarithm of the number of symbols in the target alphabet.

A fair coin has an entropy of one bit. However, if the coin is not fair, then the uncertainty is lower (if asked to bet on the next outcome, we would bet preferentially on the most frequent result), and thus the Shannon entropy is lower. Mathematically, a coin flip is an example of a Bernoulli trial, and its entropy is given by the binary entropy function. A long string of repeating characters has an entropy rate of 0, since every character is predictable. The entropy rate of English text is between 1.0 and 1.5 bits per letter,^[1] or as low as 0.6 to 1.3 bits per letter, according to estimates by Shannon based on human experiments.^[2]

Contents [hide]

- Definition
- Characterization
 - Continuity
 - Symmetry
 - Maximum
 - Additivity
- Entropy explained
- Example

Entropy (information theory) - Wikipedia, the free encyclopedia - Windows Internet Explorer

http://en.wikipedia.org/wiki/Entropy_(information_theory)

W Entropy (information the... | W Self-information - Wikipedi... | W Redundancy (information t...

Search

Navigation

- About Wikipedia
- Community portal
- Recent changes
- Contact Wikipedia
- Donate to Wikipedia
- Help

Tools

- What links here
- Related changes
- Upload file
- Special pages
- Printable version
- Permanent link
- Cite this page

Definition

The entropy H of a discrete random variable X with possible values $\{x_1, \dots, x_n\}$ is

$$H(X) = E(I(X)).$$

Here E is the expected value function, and $I(X)$ is the information content or *self-information* of X.

$I(X)$ is itself a random variable. If p_i denotes the probability mass function of X then the entropy can explicitly be written as

$$H(X) = \sum_{i=1}^n p(x_i) I(x_i) = - \sum_{i=1}^n p(x_i) \log_b p(x_i),$$

where b is the base of the logarithm used. Common values of b are 2, Euler's number e , and 10, and the unit of entropy is bit for $b = 2$, nat for $b = e$, and dit (or digit) for $b = 10$.^[1]

In the case of $p_i = 0$ for some i , the value of the corresponding summand $0 \log_b 0$ is taken to be 0, which is consistent with the limit

$$\lim_{p \rightarrow 0^+} p \log p = 0.$$

Characterization

Shannon entropy is characterized by a small number of criteria, listed below. Any definition of entropy satisfying these assumptions has the form

$$-K \sum_{i=1}^n p_i \log p_i$$

where K is a constant corresponding to a choice of measurement units.

In the following, $p_i = \Pr(X = x_i)$ and $H_n(p_1, \dots, p_n) = H(X)$

Continuity

The measure should be *continuous*, so that changing the values of the probabilities by a very small amount should only change the entropy by a small amount.

Symmetry

Redundancy (information theory) - Wikipedia, the free encyclopedia - windows internet explorer

http://en.wikipedia.org/wiki/Redundancy_(information_theory)

W: Redundancy (information theory) | discussion | edit this page | history

Log in / create account

Redundancy (information theory)

From Wikipedia, the free encyclopedia

Redundancy in information theory is the number of bits used to transmit a message minus the number of bits of actual information in the message. Informally, it is the amount of wasted "space" used to transmit certain data. Data compression is a way to reduce or eliminate unwanted redundancy, while checksums are a way of adding desired redundancy for purposes of error detection when communicating over a noisy channel of limited capacity.

Contents [hide]

- Quantitative definition
- Other notions of redundancy
- See also
- References

Quantitative definition [edit]

In describing the redundancy of raw data, recall that the rate of a source of information is the average entropy per symbol. For memoryless sources, this is merely the entropy of each symbol, while, in the most general case of a stochastic process, it is

$$r = \lim_{n \rightarrow \infty} \frac{1}{n} H(M_1, M_2, \dots, M_n),$$

the limit, as n goes to infinity, of the joint entropy of the first n symbols divided by n . It is common in information theory to speak of the "rate" or "entropy" of a language. This is appropriate, for example, when the source of information is English prose. The rate of a memoryless source is simply $H(M)$, since by definition there is no interdependence of the successive messages of a memoryless source.

The absolute rate of a language or source is simply

$$R = \log |M|,$$

the logarithm of the cardinality of the message space, or alphabet. (This formula is sometimes called the Hartley function.) This is the maximum possible rate of information that can be transmitted with that alphabet. (The logarithm should be taken to a base

Redundancy Image Processing & Computer Graphics 14

Let n_1, n_2 denote data units carrying the same information.

Relative data redundancy is given by:

$$R_D = 1 - 1/C_R$$

where C_R is termed the **compression ratio**:

$$C_R = n_1 / n_2$$

for $n_1 = n_2$: $C_R = 1$; $R = 0$
 for $n_1 \gg n_2$: $C_R \rightarrow \infty$; $R \rightarrow 1$
 for $n_1 \ll n_2$: $C_R \rightarrow 0$; $R \rightarrow -\infty$

KAPITAL LUDZKI
 Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
 UNIA EUROPEJSKA FUNDUSZ SPOŁECZNY

Interpixel redundancy removal Image Processing & Computer Graphics 15

Gray levels of adjacent pixels are strongly correlated.

Run length encoding (RLE) – an image is coded by symbol pairs (g_i, l_i) where g_i denotes i -th gray level and l_i is the run length

1	2	3	4	3	
0		2			


RL sequences: (1,4); (3,3); (0,2); (2,5); (3,2); (0,7); (3,11); (1,2)
 8*3=24 bytes are needed for image coding
 g – coded by 1 byte,
 l – coded by 2 bytes

6x6=36 bytes
 $C_R = 36/24 = 1.5$

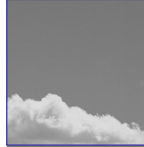
KAPITAL LUDZKI
 Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
 UNIA EUROPEJSKA FUNDUSZ SPOŁECZNY

Image Processing & Computer Graphics 19

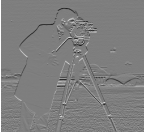
Predictive coding - example



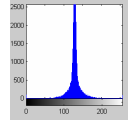
$E = 7.01$

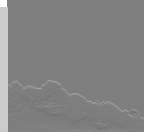


$E = 5.31$



$E = 5.06$





$E = 2.44$

KAPITAŁ LUDZKI

Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego

UNIA EUROPEJSKA FUNDUSZ SPÓŁECZNY

Image Processing & Computer Graphics 20

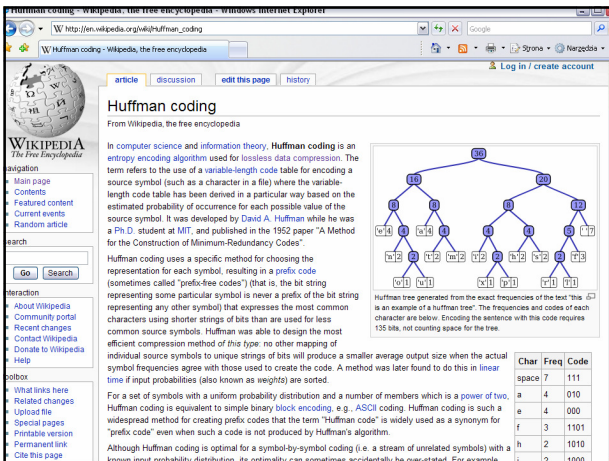
Variable length coding (Example)

l_k	$p(l_k)$	code 1	$m^1(l_k)$	code 2	$m^2(l_k)$
0	0.19	000	3	11	2
1	0.25	001	3	01	2
2	0.21	010	3	10	2
3	0.16	011	3	001	3
4	0.08	100	3	0001	4
5	0.06	101	3	00001	5
6	0.03	110	3	000001	6
7	0.02	111	3	000000	6

KAPITAŁ LUDZKI

Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego

UNIA EUROPEJSKA FUNDUSZ SPÓŁECZNY



Huffman coding

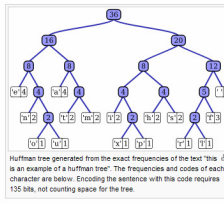
From Wikipedia, the free encyclopedia

In computer science and information theory, **Huffman coding** is an entropy encoding algorithm used for lossless data compression. The term refers to the use of a variable-length code table for encoding a source symbol (such as a character in a file) where the variable-length code table has been derived in a particular way based on the estimated probability of occurrence for each possible value of the source symbol. It was developed by David A. Huffman while he was a Ph.D. student at MIT, and published in the 1952 paper "A Method for the Construction of Minimum-Redundancy Codes".

Huffman coding uses a specific method for choosing the representation for each symbol, resulting in a prefix code (sometimes called "prefix-free codes") that is, the bit string representing some particular symbol is never a prefix of the bit string representing any other symbol) that expresses the most common characters using shorter strings of bits than are used for less common source symbols. Huffman was able to design the most efficient compression method of this type: no other mapping of individual source symbols to unique strings of bits will produce a smaller average output size when the actual symbol frequencies agree with those used to create the code. A method was later found to do this in linear time if input probabilities (also known as weights) are sorted.

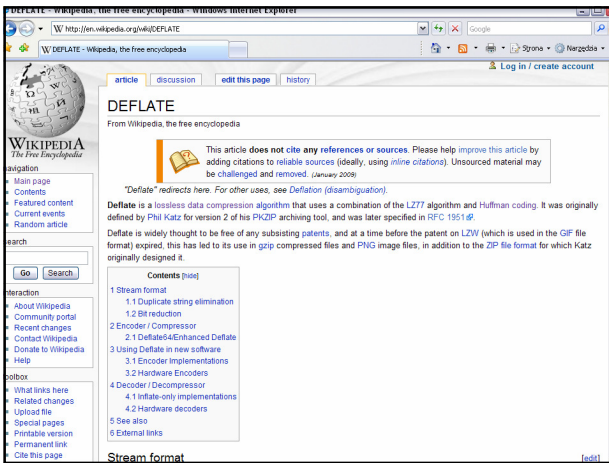
For a set of symbols with a uniform probability distribution and a number of members which is a power of two, Huffman coding is equivalent to simple binary block encoding, e.g., ASCII coding. Huffman coding is such a widespread method for creating prefix codes that the term "Huffman code" is widely used as a synonym for "prefix code" even when such a code is not produced by Huffman's algorithm.

Although Huffman coding is optimal for a symbol-by-symbol coding (i.e. a stream of unrelated symbols) with a known, almost probability distribution, the optimality can sometimes be significantly improved. *See example.*



Huffman tree generated from the exact frequencies of the text "this is an example of a Huffman tree". The frequencies and codes of each character are below. Encoding the sentence with this code requires 135 bits, not counting space for the tree.

Char	Freq	Code
space	7	111
a	4	010
e	4	000
f	3	1101
h	2	1010
t	2	1000



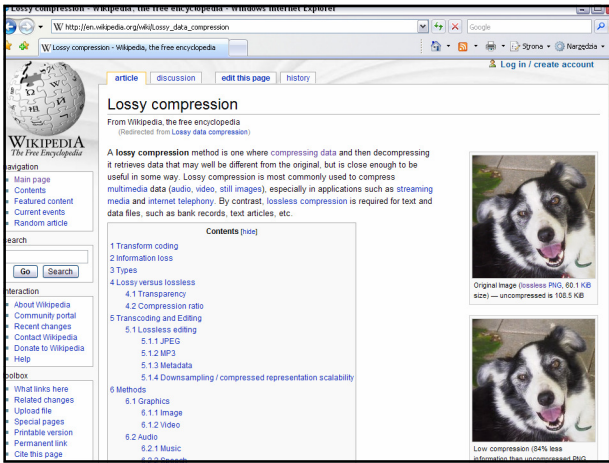


Image Processing & Computer Graphics
24

Psychovisual redundancy

Visual perception of humans does not work as a camera of a predefined characteristic.
The eye is not equally sensitive to all image features, e.g. the Mach bands

Projekt współfinansowany przez Unię Europejską
w ramach Europejskiego Funduszu Społecznego

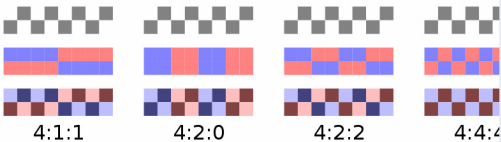
Sampling systems and ratios

The subsampling scheme is commonly expressed as a three part ratio $J:A:B$ (e.g. 4:2:2), although sometimes expressed as four parts (e.g. 4:2:2:4), that describe the number of luma and chrominance samples in a conceptual region that is J pixels wide, and 2 pixels high. The parts are (in their respective order):

- J horizontal sampling reference (width of the conceptual region). Usually, 4.
- A number of chrominance samples (C_r , C_b) in the first row of J pixels.
- B number of (additional) chrominance samples (C_r , C_b) in the second row of J pixels.
- Alpha horizontal factor (relative to first digit). May be omitted if alpha component is not present, and is equal to J when present.

An explanatory image of different chroma subsampling schemes can be seen at the following link:
<http://lea.hamradio.si/~s51kg/subsample.gif> (source: "Basics of Video"; <http://lea.hamradio.si/~s51kg/V-BAS.HTM>) or in details in Chrominance Subsampling in Digital Images.

To calculate required bandwidth factor relative to 4:4:4 (or 4:4:4:4), one needs to sum all the factors and divide the result by 12 (or 16, if alpha is present).

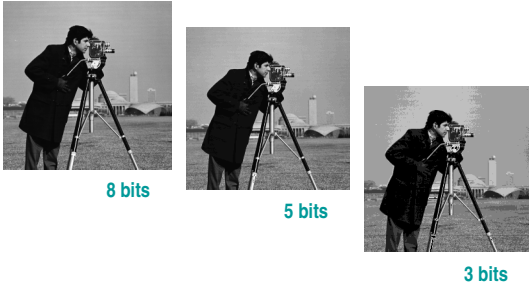


4:1:1 4:2:0 4:2:2 4:4:4

The mapping examples given are only theoretical and for illustration. Also note that the diagram does not indicate any chroma filtering, which should be applied to avoid aliasing.

Types of subsampling

Grey levels quantization



8 bits 5 bits 3 bits

KAPITAŁ LUDZKI
 Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
 UNIA EUROPEJSKA
 FUNDUSZ SPOŁECZNY

Posterization

From Wikipedia, the free encyclopedia

Posterization of an image occurs when a region of an image with a continuous gradation of tone is replaced with several regions of fewer tones, resulting in an abrupt change from one tone to another. This creates an effect somewhat similar to that of a simple graphic poster.

Contents [hide]

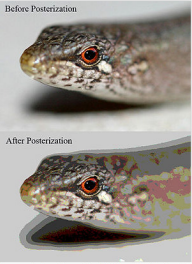
- Cause
- Definition
- Applications
- Posterizing time
- See also
- References
- External links and sources

Cause

The effect may be created deliberately, or happen accidentally.

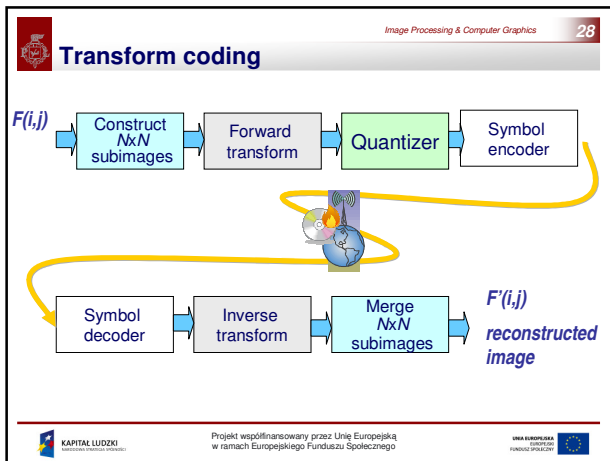
As an artistic effect, posterization may be created deliberately using most photo-editing programs.

Unwanted posterization, also known as **banding**, may occur when the color depth, sometimes called bit depth, is insufficient to accurately sample a continuous gradation of color tone. As a result, a continuous gradient appears as a series of discrete steps or bands of color — hence the name. When discussing fixed-pixel displays, such as LCD and plasma televisions, this effect is referred to as **false contouring**! The result may be compounded further by an optical illusion, called the Mach band illusion, in



Before Posterization
 After Posterization

An example of a photograph in JPEG format (24-bit color or 16.7 million colors) before posterization, contrasting the result of saving to GIF format (256 colors). Posterization occurs across the image, but is most obvious in areas of subtle variation in tone.



- Image Processing & Computer Graphics 29
- ### Image transforms
- Fourier Transform - impractical
 - The Karhunen-Loeve expansion - minimizes the mean square reconstruction error, computationally complex, no fast transform
 - Discrete Cosine Transform (DCT) – high compression ratios achievable (fast vanishing of cosine coefficients), fast transform exists
 - The wavelet transform – new compression methods developed, competitive or better than DCT, fast transform exists
- KAPITAL LUDZKI
Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
UNIA EUROPEJSKA FUNDUSZ SPÓLNY

Windows Internet Explorer

http://en.wikipedia.org/wiki/Karhunen-L%C3%B6ve_transform

W Karhunen-Loeve theorem - Wikipedia, the free encyclo...

article | discussion | edit this page | history

Karhunen–Loève theorem

From Wikipedia, the free encyclopedia
(Redirected from Karhunen-Loeve transform)

In the theory of stochastic processes, the **Karhunen-Loève theorem** (named after **Kari Karhunen** and **Michel Loève**) is a representation of a function on a bounded interval. In contrast to a Fourier series where the coefficients are real numbers and the expansion basis consists of sinusoidal functions (that is, sine and cosine functions), the coefficients in the Karhunen-Loève theorem are random variables and the expansion basis depends on the process. In fact, the orthogonal basis functions used in this representation are determined by the covariance function of the process. If we regard a stochastic process as a random function F , that is, one in which the random value is a function on an interval $[a, b]$, then this theorem can be considered as a random orthogonal expansion of F .

In the case of a centered stochastic process $\{X_t\}_{t \in [a, b]}$ (where centered means that the expectations $E\{X_t\}$ are defined and equal to 0 for all values of the parameter t in $[a, b]$) satisfying a technical continuity condition, admits a decomposition

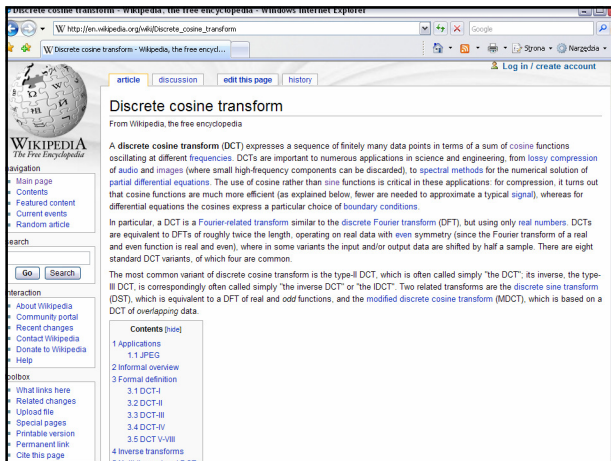
$$X_t = \sum_{k=1}^{\infty} Z_k e_k(t),$$

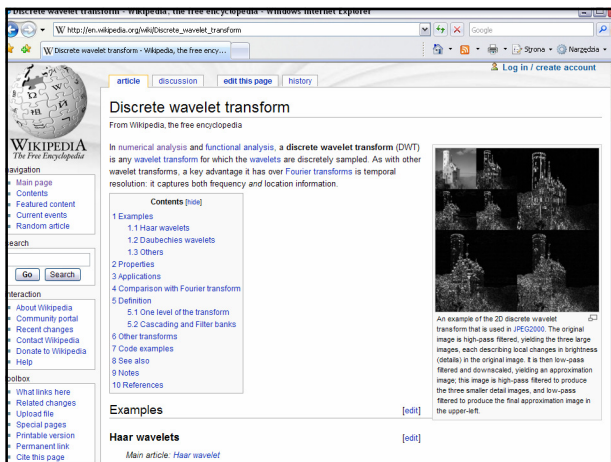
where Z_k are pairwise uncorrelated random variables and the functions e_k are continuous real-valued functions on $[a, b]$ which are pairwise orthogonal in $L^2([a, b])$. The general case of a process which is not centered can be represented by expanding the expectation function (which is a non-random function) in the basis e_k .

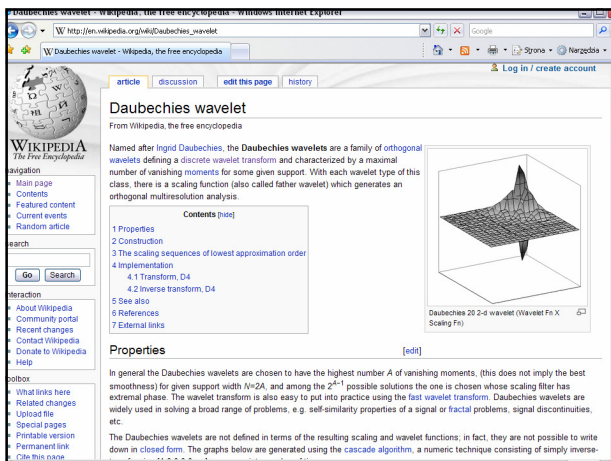
Moreover, if the process is Gaussian, then the random variables Z_k are Gaussian and stochastically independent. This result generalizes the Karhunen-Loève transform. An important example of a centered real stochastic process on $[0,1]$ is the Wiener process and the Karhunen-Loève theorem can be used to provide a canonical orthogonal representation for it. In this case the expansion consists of sinusoidal functions.

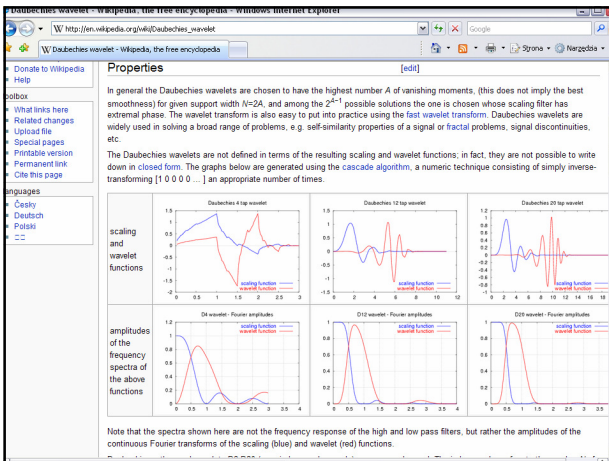
The above expansion into uncorrelated random variables is also known as the Karhunen-Loève expansion or Karhunen-Loève decomposition. The empirical version (i.e., with the coefficients computed from a sample) is known as Principal component analysis, Proper orthogonal decomposition (POD), or the Hotelling transform.

Contents [hide]









Cohen-Daubechies-Feauveau wawelet - Wikipedia, the free encyclopedia

W Cohen-Daubechies-Feauveau wawelet - Wikipedia, th...

article | discussion | edit this page | history

Cohen-Daubechies-Feauveau wawelet

From Wikipedia, the free encyclopedia

For other uses of "CDF", see CDF (disambiguation).

Cohen-Daubechies Feauveau wawelet are the historically first family of biorthogonal wawellets, which was made popular by Ingrid Daubechies. These are not the same as the orthogonal Daubechies wawellets, and also not very similar in shape and properties. However their construction idea is the same.

The JPEG 2000 compression standard uses the biorthogonal CDF 5/3 wawelet (also called the **LeGall 5/3 wawelet**) for lossless compression and a CDF 9/7 wawelet for lossy compression.

Contents [hide]

- 1 Properties
- 2 Construction
- 3 Tables of coefficients
- 4 Numbering
- 5 Lifting decomposition
 - 5.1 Even number of smoothness factors
 - 5.2 Odd number of smoothness factors
- 6 Literature

Properties [edit]

- The **primal generator** is a B-spline if the simple factorization $\phi_{primal}(x) = 1$ (see below) is chosen
- The **dual generator** has the maximum number of smoothness factors which is possible for its length.
- All generators and wawellets in this family are symmetric.

Construction [edit]

An example of the 20-wavelet transform from the LeGall 5/3 wavelet used in JPEG2000

DCT basis functions

Image Processing & Computer Graphics 36

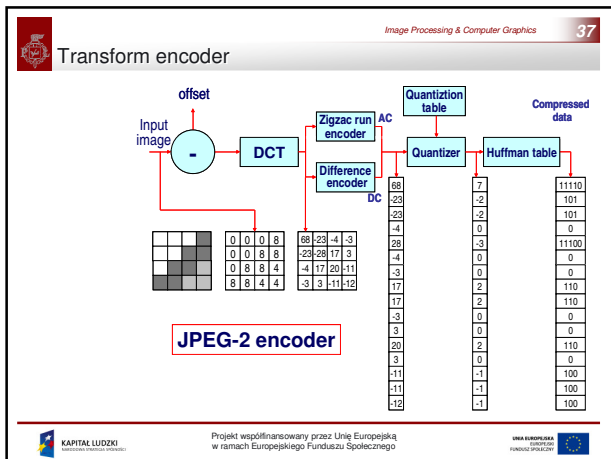
DCT coefficients of image blocks assign a weight to each of the basis functions

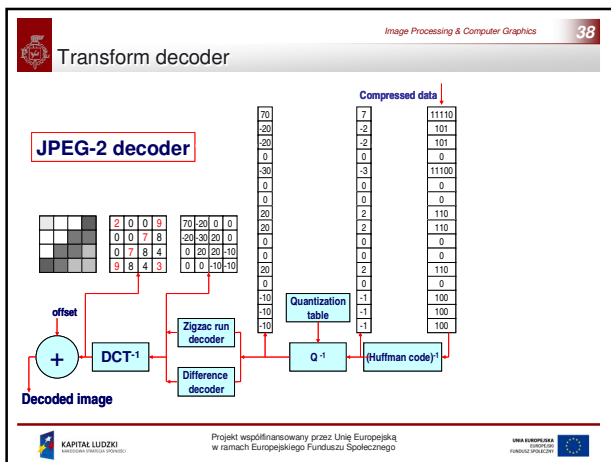
Image 8x8 blocks are obtained by computing a linear combination of these DCT basis functions

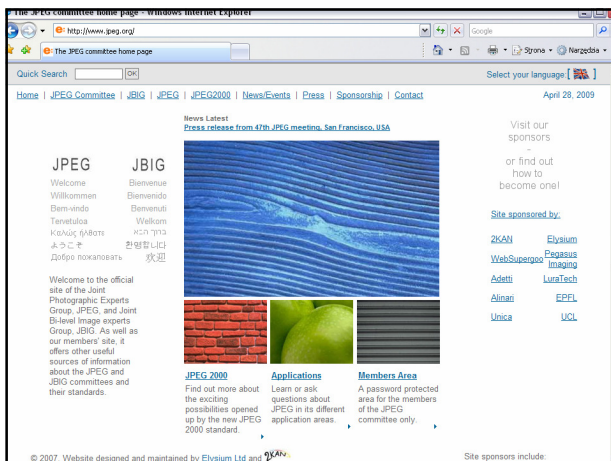
KAPITAŁ LUDZKI
WIOSNA PRZEKAZU WIEDZY

Projekt współfinansowany przez Unię Europejską
w ramach Europejskiego Funduszu Społecznego

UNA EUROPEJSKA
WIOSNA PRZEKAZU WIEDZY







Wikipedia, the free encyclopedia - Windows Internet Explorer

Wikipedia, the free encyclopedia

article | discussion | edit this page | history

JPEG

From Wikipedia, the free encyclopedia

This article is about the image coding standard that is informally referred to as "JPEG", which is an acronym for the name of the committee that created the standard; for information about the committee, please refer to the *Joint Photographic Experts Group* article.

"JPG" redirects here. For the magazine, see *JPG (magazine)*.

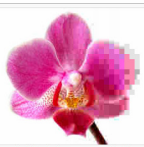
In computing, **JPEG** (pronounced /dʒɛɪpeɪɡɪˈdʒeɪpeɪ/, *JAY-peg*) is a commonly used method of compression for photographic images. The degree of compression can be adjusted, allowing a selectable tradeoff between storage size and image quality. JPEG typically achieves 10:1 compression with little perceptible loss in image quality.

JPEG compression is used in a number of image file formats. JPEG*EX* is the most common image format used by digital cameras and other photographic image capture devices; along with JPEG/JFIF, it is the most common format for storing and transmitting photographic images on the World Wide Web. These format variations are often not distinguished, and are simply called JPEG.

The MIME media type for JPEG is *image/jpeg* (defined in RFC 1341 [d]).

Contents (hide)

- 1 The JPEG standard
- 2 Typical usage
- 3 JPEG compression
 - 3.1 Lossless editing
- 4 JPEG files
 - 4.1 JPEG file extensions
 - 4.2 Color profile
- 5 Syntax and structure
- 6 JPEG code sample
- 6.1 Encoding



JPEG

A photo of a flower compressed with successively more lossy compression ratios from left to right.

Filename	.jpg, .jpeg, .jpe
Extension	.jpg, .jpeg, .jpe (contains*)
Internet media type	image/jpeg
Type code	jpg



Wikipedia, the free encyclopedia - Windows Internet Explorer

Wikipedia, the free encyclopedia

particular option is a lossy data compression method.

Color space transformation

First, the image should be converted from RGB into a different color space called YCbCr. It has three components Y, Cb and Cr; the Y component represents the brightness of a pixel, the Cb and Cr components represent the chrominance (split into blue and red components). This is the same color space as used by digital color television as well as digital video including video DVD's, and is similar to the way color is represented in analog PAL video and MAC, but not by analog NTSC, which uses the YIQ color space. The YCbCr color space conversion allows greater compression without a significant effect on perceptual image quality (or greater perceptual image quality for the same compression). The compression is more efficient as the brightness information, which is more important to the eventual perceptual quality of the image, is confined to a single channel, more closely representing the human visual system.

This conversion to YCbCr is specified in the JFIF standard, and should be performed for the resulting JPEG file to have maximum compatibility. However, some JPEG implementations in "highest quality" mode do not apply this step and instead keep the color information in the RGB color model^[*citation needed*], where the image is stored in separate channels for red, green and blue luminance. This results in less efficient compression, and would not likely be used if file size was an issue.

Downsampling

Due to the densities of color- and brightness-sensitive receptors in the human eye, humans can see considerably more fine detail in the brightness of an image (the Y component) than in the color of an image (the Cb and Cr components). Using this knowledge, encoders can be designed to compress images more efficiently.

The transformation into the YCbCr color model enables the next step, which is to reduce the spatial resolution of the Cb and Cr components (called "downsampling" or "chroma subsampling"). The ratios at which the downsampling can be done on JPEG are 4:4:4 (no downsampling), 4:2:2 (reduce by factor of 2 in horizontal direction), and most commonly 4:2:0 (reduce by factor of 2 in horizontal and vertical directions). For the rest of the compression process, Y, Cb and Cr are processed separately and in a very similar manner.

Block splitting

After subsampling, each channel must be split into 8×8 blocks of pixels. Depending on chroma subsampling, this yields (Minimum Coded Unit) MCU blocks of size 8×8 (4:4:4 – no subsampling), 16×8 (4:2:2), or most commonly 16×16 (4:2:0).

If the data for a channel does not represent an integer number of blocks then the encoder must fill the remaining area of the incomplete blocks with some form of dummy data. Filling the edge pixels with a fixed color (typically black) creates ringing artifacts along the visible part of the border; repeating the edge pixels is a common technique that reduces the visible border, but it can still create artifacts.



Wikipedia, the free encyclopedia - Windows Internet Explorer

Wikipedia, the free encyclopedia

Block splitting

After subsampling, each channel must be split into 8×8 blocks of pixels. Depending on chroma subsampling, this yields (Minimum Coded Unit) MCU blocks of size 8×8 (4:4:4 – no subsampling), 16×8 (4:2:2), or most commonly 16×16 (4:2:0).

If the data for a channel does not represent an integer number of blocks then the encoder must fill the remaining area of the incomplete blocks with some form of dummy data. Filling the edge pixels with a fixed color (typically black) creates ringing artifacts along the visible part of the border; repeating the edge pixels is a common technique that reduces the visible border, but it can still create artifacts.

Discrete cosine transform

Next, each component (Y, Cb, Cr) of each 8×8 block is converted to a frequency-domain representation, using a normalized, two-dimensional type-II discrete cosine transform (DCT).

As an example, one such 8×8 bit subimage might be:

52	55	61	66	70	61	64	73
63	59	55	90	109	85	69	72
62	59	68	113	144	104	66	73
63	58	71	122	154	106	70	69
67	61	68	104	126	88	68	70
79	65	60	70	77	68	58	75
85	71	64	59	55	61	65	83
87	79	69	68	65	76	78	94

The 8×8 sub-image shown in 6-bit grayscale

Before computing the DCT of the subimage, its gray values are shifted from a positive range to one centered around zero. For an 8-bit image each pixel has 256 possible values: [0,255]. To center around zero it is necessary to subtract by half the number of possible values, or 128.

$$\frac{256}{2} = \frac{2^8}{2} = 2^7 = 128$$

Subtracting 128 from each pixel value yields pixel values on [−128,127]



range to one centered around zero. For an 8-bit image each pixel has 256 possible values: [0..255]. To center around zero it is necessary to subtract by half the number of possible values, or 128.

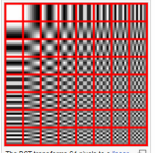
$$\frac{2^8}{2} = \frac{256}{2} = 2^7 = 128$$

Subtracting 128 from each pixel value yields pixel values on [-128..127]

-76	-73	-67	-62	-58	-67	-64	-55
-65	-69	-73	-38	-19	-43	-59	-56
-66	-69	-60	-15	16	-24	-62	-55
-65	-70	-57	-6	26	-22	-58	-59
-61	-67	-60	-24	-2	-40	-60	-58
-49	-63	-68	-58	-51	-60	-70	-53
-43	-57	-64	-69	-73	-67	-63	-45
-41	-49	-59	-60	-63	-52	-50	-34

}
y

The next step is to take the two-dimensional DCT, which is given by:



The DCT matrix is a 2D grid of values, with a color gradient from dark red to light yellow. A red box highlights the top-left corner of the matrix, indicating the region of highest energy.

Quantization

The human eye is good at seeing small differences in brightness over a relatively large area, but not so good at distinguishing the exact strength of a high frequency brightness variation. This allows one to greatly reduce the amount of information in the high frequency components. This is done by simply dividing each component in the frequency domain by a constant for that component, and then rounding to the nearest integer. This is the main lossy operation in the whole process. As a result of this, it is typically the case that many of the higher frequency components are rounded to zero, and many of the rest become small positive or negative numbers, which take many fewer bits to store.

A typical quantization matrix, as specified in the original JPEG Standard^[9], is as follows:

$$\begin{bmatrix} 16 & 11 & 10 & 16 & 24 & 40 & 51 & 61 \\ 12 & 12 & 14 & 19 & 26 & 58 & 60 & 55 \\ 14 & 13 & 16 & 24 & 40 & 57 & 69 & 56 \\ 14 & 17 & 22 & 29 & 51 & 87 & 80 & 62 \\ 18 & 22 & 37 & 56 & 68 & 109 & 103 & 77 \\ 24 & 35 & 55 & 64 & 81 & 104 & 113 & 92 \\ 49 & 64 & 78 & 87 & 103 & 121 & 120 & 101 \\ 72 & 92 & 95 & 98 & 112 & 100 & 103 & 99 \end{bmatrix}$$

The quantized DCT coefficients are computed with

$$B_{j,k} = \text{round}\left(\frac{G_{j,k}}{Q_{j,k}}\right) \text{ for } j = 0, 1, 2, \dots, N_1 - 1; k = 0, 1, 2, \dots, N_2 - 1$$

where G is the unquantized DCT coefficients, Q is the quantization matrix above, and B is the quantized DCT coefficients. (Note that this is in **no way** matrix multiplication.)

Using this quantization matrix with the DCT coefficient matrix from above results in:

$$\begin{bmatrix} -26 & -3 & -6 & 2 & 2 & -1 & 0 & 0 \\ 0 & -2 & -4 & 1 & 1 & 0 & 0 & 0 \\ -3 & 1 & 5 & -1 & -1 & 0 & 0 & 0 \\ -4 & 1 & 2 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Entropy coding

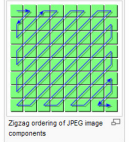
Main article: [Entropy encoding](#)

Entropy coding is a special form of lossless data compression. It involves arranging the image components in a "zigzag" order employing run-length encoding (RLE) algorithms that groups similar frequencies together, inserting length coding zeros, and then using Huffman coding, as what is left. The JPEG standard also allows, but does not require, the use of arithmetic coding, which is mathematically superior to Huffman coding. However, this feature is rarely used as it is covered by patents and because it is much slower to encode and decode compared to Huffman coding. Arithmetic coding typically makes files about 5% smaller.

The zigzag sequence for the above quantized coefficients are shown below. (The format shown is just for ease of understanding/viewing.)

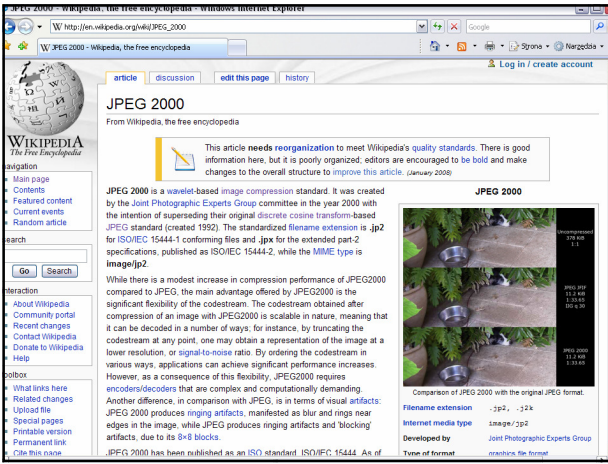
```

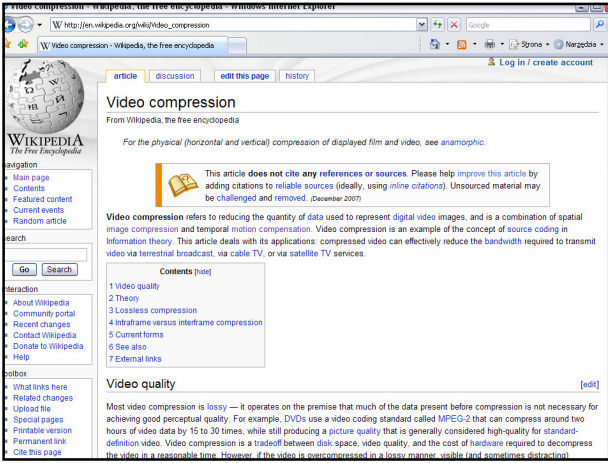
-26
-3 0
-3 -2 -6
2 -4 1 -4
1 1 5 1 2
-1 1 -1 2 0 0
0 0 0 -1 -1 0 0 0
0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0
0 0 0
0 0
0
  
```

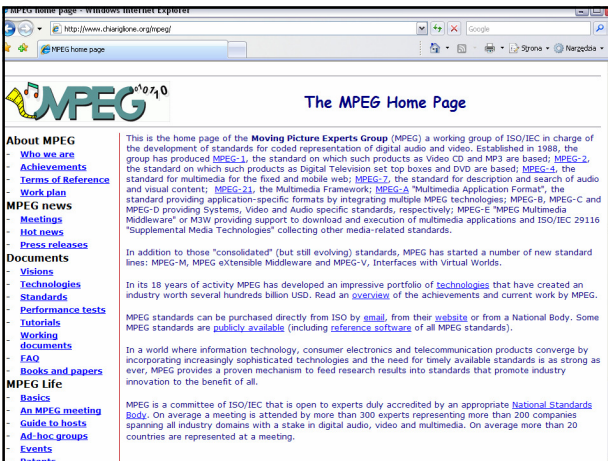


Zigzag ordering of JPEG image components

If the i th block is represented by B_i and positions within each block are represented by (p, q) where $p = 0, 1, \dots, 7$ and $q = 0, 1, \dots, 7$.







Moving Picture Experts Group - Wikipedia, the free encyclopedia - Windows Internet Explorer

Wikipedia, the free encyclopedia

article | discussion | edit this page | history

Moving Picture Experts Group

From Wikipedia, the free encyclopedia
(redirected from MPEG)

"MPEG" redirects here. For the Motion Picture Editors Guild also known as MPEG, see *Motion Picture Editors Guild*.

The **Moving Picture Experts Group** (acronym: **MPEG**) was formed by the ISO to set standards for audio and video compression and transmission.^[1] Its first meeting was in May 1988 in Ottawa, Canada. As of late 2005, MPEG has grown to include approximately 350 members per meeting from various industries, universities, and research institutions. MPEG's official designation is ISO/IEC JTC1/SC29 WG11.

Contents [hide]

- Overview
- Standards
- See also
- Notes
- External links

Overview

The MPEG compression methodology is considered as asymmetric—where the encoder is more complex than the decoder.^[2] The encoder needs to be *algorithmic* or *adaptive* whereas the decoder is "dumb" and carries out fixed actions.^[2] This is considered advantageous in applications such as broadcasting where the number of expensive complex encoders are small but the number of simple inexpensive decoders is large. This approach of the ISO to standardization in MPEG is considered novel because it is not the encoder which is standardized, instead, the way in which a decoder shall interpret the bitstream is defined. A decoder which can successfully interpret the bitstream is said to be compliant.^[2] The advantage of standardizing the decoder is that over time encoding algorithms can improve yet compliant decoders will continue to function with them.^[2]

Compression methodology 57



Moving Picture Experts Group - Wikipedia, the free encyclopedia - Windows Internet Explorer

Wikipedia, the free encyclopedia

article | discussion | edit this page | history

MPEG-1

From Wikipedia, the free encyclopedia

The MPEG standards consist of different Parts. Each part covers a certain aspect of the whole specification.^[1] The standards also specifies Profiles and Levels. Profiles are intended to define a set of tools that are available, and Levels define the range of appropriate values for the properties associated with them.^[1] MPEG has standardized the following compression formats and ancillary standards:

- MPEG-1 is the first compression standard for audio and video. It was basically designed to allow moving pictures and sound to be encoded into the bitrate of a Compact Disc. To meet the low bit requirement, MPEG-1 downsamples the images, as well as using picture rates of only 24-30 Hz, resulting in a moderate quality.^[1] It includes the popular Layer 3 (MP3) audio compression format.
- MPEG-2 Transport, video and audio standards for broadcast-quality television. MPEG-2 standard was considerably broader in scope and of wider appeal—supporting interlacing and high definition. MPEG-2 is considered important because it has been chosen as the compression scheme for over-the-air digital television ATSC, DVB and ISDB; digital satellite TV services like Dish Network; digital cable television signals, SVCD, and DVD.^[1]
- MPEG-3. Developments in standardizing scalable and multi-resolution compression which would have become MPEG-3 were ready by the time MPEG-2 was to be standardized; hence, these were incorporated into MPEG-2 and as a result there is no MPEG-3 standard.^[1] MPEG-3 is not to be confused with MP3, which is MPEG-1 Audio Layer 3.
- MPEG-4. MPEG-4 uses further coding tools with additional complexity to achieve higher compression factors than MPEG-2.^[1] In addition to more efficient coding of video, MPEG-4 moves closer to computer graphics applications. In more complex profiles, the MPEG-4 decoder effectively becomes a rendering processor and the compressed bitstream describes three-dimensional shapes and surface texture.^[1] MPEG-4 also provides Intellectual Property Management and Protection (IPMP) which provides the facility to use proprietary technologies to manage and protect content like digital rights management.^[1] Several new higher-efficiency video standards (fewer than MPEG-2 Video) are included (an alternative to MPEG-2 Video), notably:
 - MPEG-4 Part 2 (or Advanced Simple Profile) and
 - MPEG-4 Part 10 (or Advanced Video Coding or H.264). MPEG-4 Part 10 may be used on HD DVD and Blu-ray discs, along with VC-1 and MPEG-2.

In addition, the following standards, while not sequential advances to the video encoding standard as with MPEG-1 through MPEG-4, are referred to by similar notation:

- MPEG-7. A multimedia content description standard.
- MPEG-21. MPEG describes this standard as a *multimedia framework*.

Moreover, relatively more recently than other standards above, MPEG has started following international standards: each of the standards holds multiple MPEG technologies for a way of application. For example, MPEG-A includes a number of technologies on multimedia application format.^[12]



MPEG-1 - Wikipedia, the free encyclopedia - Windows Internet Explorer

Wikipedia, the free encyclopedia

article | discussion | edit this page | history

MPEG-1

From Wikipedia, the free encyclopedia

MPEG-1 is a standard for lossy compression of video and audio. It is designed to compress VHS-quality raw digital video and CD audio down to 1.5 Mbit/s (26:1 and 6:1 compression ratios respectively)^[1] without excessive quality loss, making Video CDs, digital cable/satellite TV and digital audio broadcasting (DAB) possible.^[2]

Today, MPEG-1 has become the most widely compatible lossy audio/video format in the world, and is used in a large number of products and technologies. Perhaps the best-known part of the MPEG-1 standard is the MP3 audio format it introduced.

The MPEG-1 standard is published as ISO/IEC-11172. The standard consists of the following five Parts:

- Systems (storage and synchronization of video, audio, and other data together)
- Video (compressed video content)
- Audio (compressed audio content)
- Conformance testing (testing the correctness of implementations of the standard)
- Reference software (example software showing how to encode and decode according to the standard)

Contents [hide]

- History
- Patents
- Applications
- Part 1: Systems
 - Elementary Streams
 - Program Streams
 - Multiplexing
- Part 2: Video
 - Color Space
 - Resolution/Bitrate
 - Frame/Picture/Block Types
 - 1:4 Frames
 - 2:2 P-Frames

Moving Picture Experts Group Phase 1 (MPEG-1)

Filename	.mpg, .mpeg, .m1,
extension	.mp1, .mp3, .m1v, .m1a, .m2a, .mpa, .mpv
Internet media type	audio/mpeg, video/mpeg
Developed by	ISO, EC
Type of format	audio, video, container
Extended from	JPEG, H.261



Wikipedia, the free encyclopedia

Part 2: Video

Part 2 of the MPEG-1 standard covers video and is defined in ISO/IEC-11172.2. It is heavily based on H.261.

MPEG-1 Video exploits perceptual compression methods to significantly reduce the data rate required by a video stream. It reduces or completely discards information in certain frequencies and areas of the picture that the human eye has limited ability to fully perceive. It also utilizes effective methods to exploit temporal (over time) and spatial (across a picture) redundancy common in video, to achieve better data compression than would be possible otherwise. (See: [Video compression](#))

Color Space

Before encoding video to MPEG-1, the color-space is transformed to YCbCr. Y= Luma, Cb=Chroma Blue, Cr=Chroma Red. Luma (brightness; resolution) is stored separately from chroma (color, hue, phase) and even further separated into red and blue components. The chroma is also subsampled to 4:2:0, meaning it is decimated by one half vertically and one half horizontally, to just one quarter the resolution of the video.^[1]

Because the human eye is much less sensitive to small changes in color than in brightness, chroma subsampling is a very effective way to reduce the amount of video data that needs to be compressed. On videos with fine detail (high spatial complexity) this can manifest as chroma aliasing artifacts. Compared to other digital compression artifacts, this issue seems to be very rarely a source of annoyance.

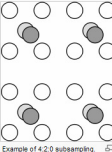
Because of subsampling, YCbCr video must always be stored using even dimensions (divisible by 2), otherwise chroma mismatch ("ghosts") will occur, and it will appear as if the color is ahead of, or behind the rest of the video, much like a shadow.

YCbCr is often inaccurately called YUV which is only used in the domain of analog video signals. Similarly, the terms luminance and chrominance are often used instead of the (more accurate) terms luma and chroma.

Resolution/Bitrate

MPEG-1 supports resolutions up to 4095x4095 (12-bits), and bitrates up to 100 Mbit/s.^[4]

MPEG-1 videos are most commonly seen using Source Input Format (SIF) resolution: 352x240, 352x288, or 320x240. These low resolutions, combined with a bitrate less than 1.5 Mbit/s, make up what is known as a **constrained parameters bitstream (CPB)**, later renamed the "Low Level" (LL) profile in MPEG-2. This is the minimum video specifications any decoder should be able to handle. To be



Example of 4:2:0 subsampling. The 2 overlapping center circles represent chroma blue and chroma red (color) planes, while the 4 outside circles represent the luma (brightness).

Wikipedia, the free encyclopedia

Macroblocks

Main article: [Macroblock](#)

MPEG-1 operates on video in a series of 8x8 blocks for quantization. However, because chroma (color) is subsampled by a factor of 4, each pair of (red and blue) chroma blocks corresponds to 4 different luma blocks. This set of 6 blocks, with a resolution of 16x16, is called a **macroblock**.

A macroblock is the smallest independent unit of (color) video. Motion vectors (see below) operate solely at the macroblock level. If the height and/or width of the video is not exact multiples of 16, a full row of macroblocks must still be encoded (though not displayed) to store the remainder of the picture (macroblock padding). This wastes a significant amount of data in the bitstream, and is to be strictly avoided.

Some decoders will also improperly handle videos with partial macroblocks, resulting in visible artifacts.

Motion Vectors

To decrease the amount of spatial redundancy in a video, only blocks that change are updated, (up to the maximum GOP size). This is known as **conditional replenishment**. However, this is not very effective by itself. Movement of the objects, and/or the camera may result in large portions of the frame needing to be updated, even though only the position of the previously encoded objects has changed. Through **motion estimation** the encoder can compensate for this movement and remove a large amount of redundant information.

The encoder compares the current frame with adjacent parts of the video from the anchor frame (previous I- or P- frame) in a diamond pattern, up to a (encoder-specific) predefined radius limit from the area of the current macroblock. If a match is found, only the direction and distance (i.e. the **vector** of the motion) from the previous video area to the current macroblock need to be encoded into the inter-frame (P- or B- frame). The reverse of this process, performed by the decoder to reconstruct the picture, is called **motion compensation**.

A predicted macroblock rarely matches the current picture perfectly, however. The differences between the estimated matching area, and the real frame/macroblock is called the **prediction error**. The larger the error, the more data must be additionally encoded in the frame. For efficient video compression, it is very important that the encoder is capable of effectively and precisely performing motion estimation.

Motion vectors record the distance between two areas on screen based on the number of pixels (called **pixels**). MPEG-1 video uses a motion vector (MV) precision of one half of one pixel, or **half-pixel**. The finer the precision of the MV's, the more accurate the match is likely to be, and the more efficient the compression. There are trade-offs to higher precision, however. Finer MV's result in larger data size, as larger numbers must be stored in the frame for every single MV, increased coding complexity as increasing levels of

Wikipedia, the free encyclopedia

Optical flow

From Wikipedia, the free encyclopedia

Optical flow or **optic flow** is the pattern of apparent motion of objects, surfaces, and edges in a visual scene caused by the relative motion between an observer (an eye or a camera) and the scene.^{[1][2]} Optical flow techniques such as motion detection, object segmentation, time-to-collision and focus of expansion calculations, motion compensated encoding, and stereo disparity measurement utilize this motion of the objects surfaces, and edges.^{[3][4]}

Contents [hide]

- 1 Estimation of the optical flow
- 1.1 Methods for determining optical flow
- 2 Uses of optical flow
- 3 References
- 4 External links

Estimation of the optical flow

Sequences of ordered images allow the estimation of motion as either instantaneous image velocities or discrete image displacements.^[5] Fleet and Weiss provide a tutorial introduction to gradient based optical flow.^[6] John L. Barron, David J. Fleet, and Steven Beauchemin provides a performance analysis of a number of optical flow techniques. It emphasizes the accuracy and density of measurements.^[7]

The optical flow methods try to calculate the motion between two image frames which are taken at times t and $t + \delta t$ at every voxel position. These methods are called differential since they are based on local Taylor series approximations of the image signal, that is: they use partial derivatives with respect to the spatial and temporal coordinates.

For a 2D+1 dimensional case (3D or n-D cases are similar) a voxel at location (x, y, t) will have moved by δx , δy and δz between the two image frames, and the following image constraint equation can be given:

$$I_x \delta x + I_y \delta y + I_t \delta t = 0$$

Image Processing & Computer Graphics 55

Block matching

- MAD - Mean Absolute Difference
- SAD - Sum of Absolute Differences
- MI - Mutual Information
- NCC - Normalized Cross-Correlation

$$MAD(x, y) = \frac{1}{MN} \sum_{m=1}^M \sum_{n=1}^N |I_{image}(x+m-\frac{M}{2}, y+n-\frac{N}{2}) - I_{block}(m, n)|$$

KAPITAŁ LUDZKI
Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
UNIA EUROPEJSKA FUNDUSZ SPÓŁECZNY

Internet Explorer

http://en.wikipedia.org/wiki/Motion_compensation

Wikipedia, the free encyclopedia

Motion compensation

From Wikipedia, the free encyclopedia

The introduction to this article provides **insufficient context** for those unfamiliar with the subject.
Please help improve the article with a good introductory style.

This article **does not cite any references or sources**. Please help improve this article by adding citations to reliable sources (ideally, using *inline citations*). Unsourced material may be challenged and removed. (December 2005)

The text in this article or section may be **incoherent or very hard to understand**, and should be reworded if the intended meaning can be determined. The *talk* page may have details.

One method used by various video formats to reduce file size is **motion compensation**. For many frames of a movie, the only difference between one frame and another is the result of either the camera moving or an object in the frame moving. In reference to a video file, this means much of the information that represents one frame will be the same as the information used in the next frame. Motion compensation takes advantage of this to provide a way to create frames of a movie from a reference frame.^[1] For example, in principle, if a movie is shot at 24 frames per second, motion compensation would allow the movie file to store the full information for every fourth frame. The only information stored for the frames in between would be the information needed to transform the previous frame into the next frame. If a frame of information is 1 MB in size, then uncompressed, one second of this film would be 24 MB in size. Applying motion compensation, the file size for one second of the film can often be reduced to 6 MB, for typical video material. More formally, in video compression, motion compensation is a technique for describing a picture in terms of the transformation of a reference picture to the current picture. The reference picture may be previous in time or even from the future. When images can be accurately synthesized from previously transmitted/stored images then the compression efficiency can be improved.

Contents [hide]

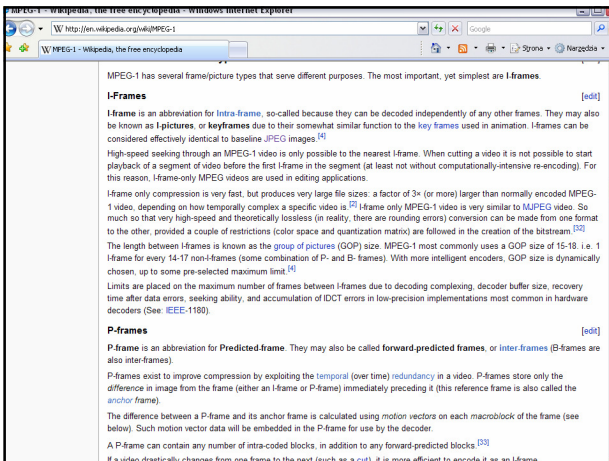
- Motion Compensation in MPEG
- Global motion compensation

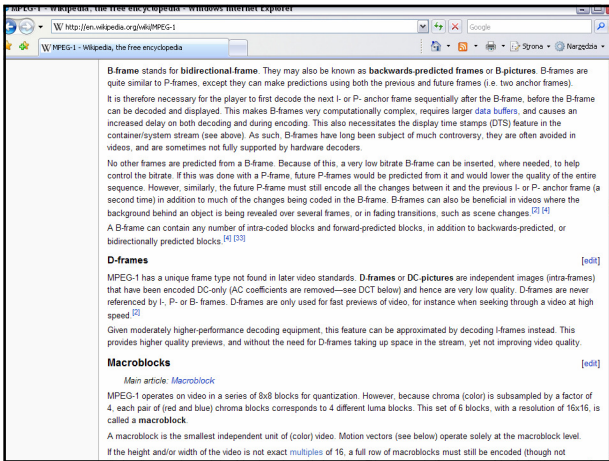
KAPITAŁ LUDZKI
Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
UNIA EUROPEJSKA FUNDUSZ SPÓŁECZNY

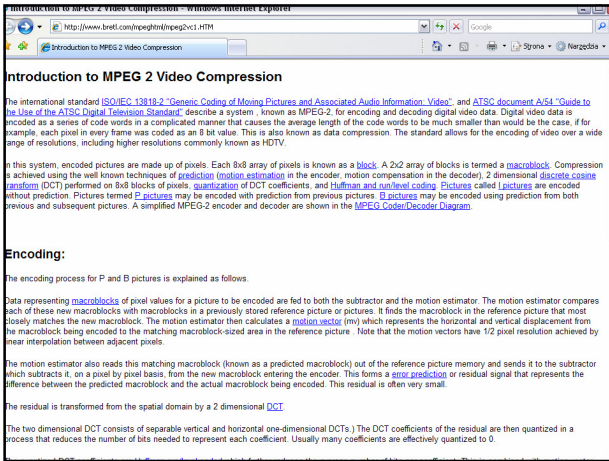
Image Processing & Computer Graphics 57

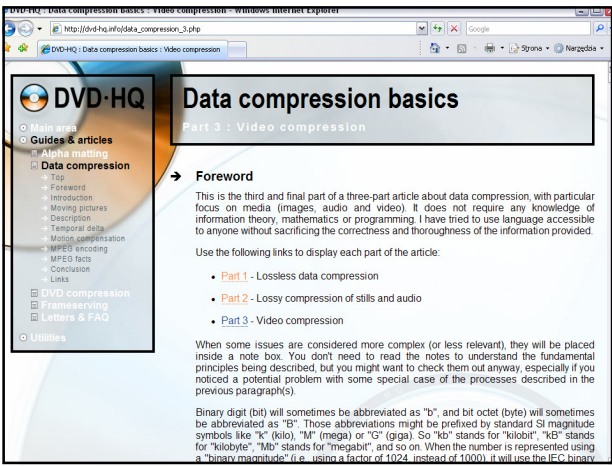
IPB frames

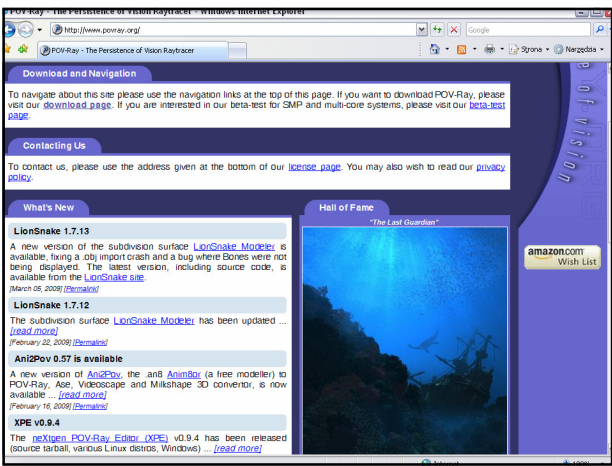
KAPITAŁ LUDZKI
Projekt współfinansowany przez Unię Europejską w ramach Europejskiego Funduszu Społecznego
UNIA EUROPEJSKA FUNDUSZ SPÓŁECZNY

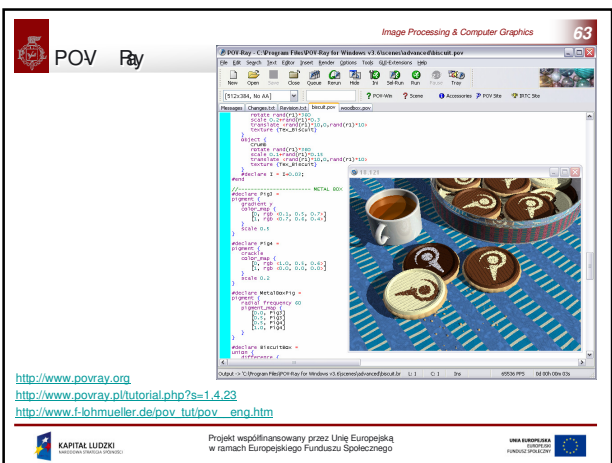


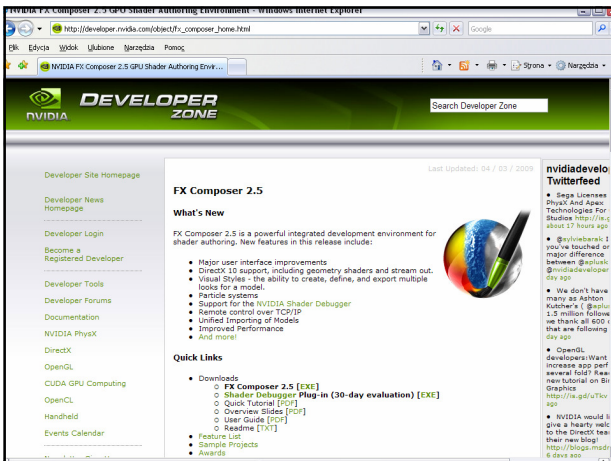
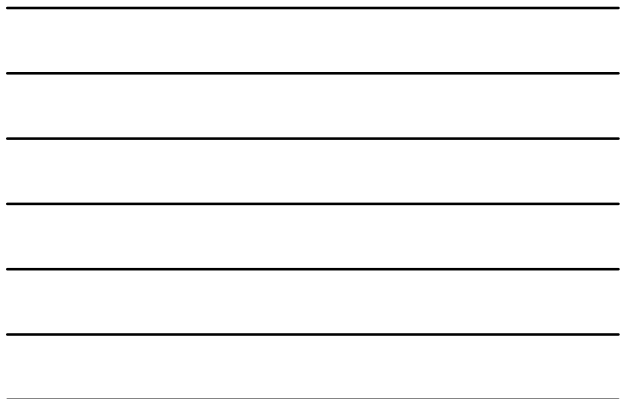
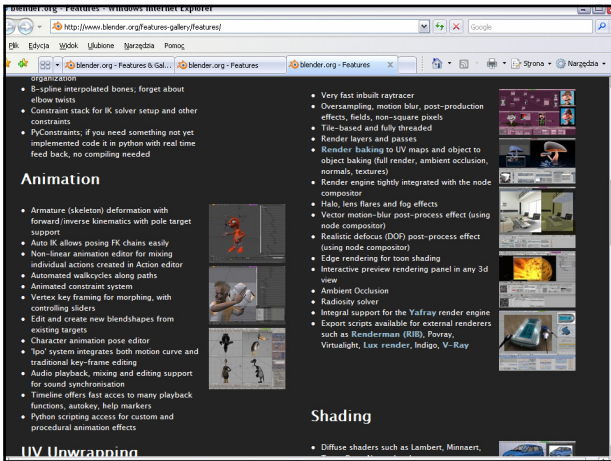
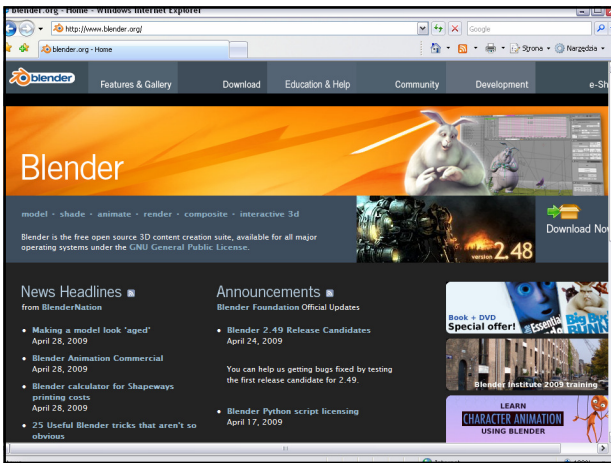












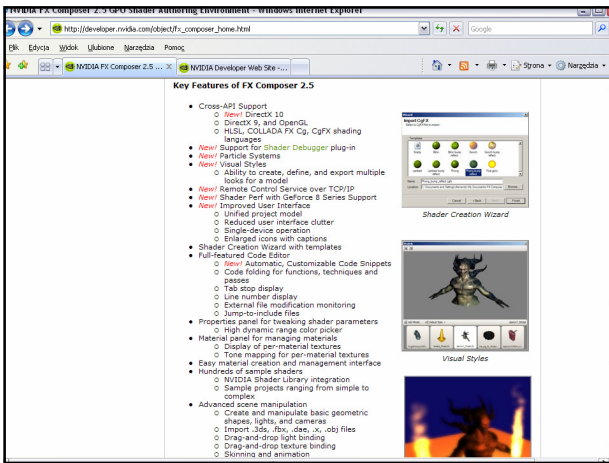


Image Processing & Computer Graphics **68**

Summary, discussion and quiz

Summary, discussion and quiz

KAPITAŁ LUDZKI
NARODOWA STRATEGIA SPÓJNOŚCI

Projekt współfinansowany przez Unię Europejską
w ramach Europejskiego Funduszu Społecznego

UNIA EUROPEJSKA
EUROPEJSKI
FUNDUSZ SPOŁECZNY

KAPITAŁ LUDZKI
NARODOWA STRATEGIA SPÓJNOŚCI

UNIA EUROPEJSKA
EUROPEJSKI
FUNDUSZ SPOŁECZNY

„Image Processing and Computer Graphics”

**Prezentacja multimedialna współfinansowana przez
Unię Europejską w ramach
Europejskiego Funduszu Społecznego w projekcie pt.
„Innowacyjna dydaktyka bez ograniczeń - zintegrowany
rozwoj Politechniki Łódzkiej - zarządzanie Uczelnia,
nowoczesna oferta edukacyjna i wzmacniania zdolności
do zatrudniania osób niepełnosprawnych”**

Politechnika Łódzka
Politechnika Łódzka, ul. Żeromskiego 116, 90-924 Łódź, tel. (042) 631 28 83
www.kapitalludzki.p.lodz.pl
